

Unit 9 Day 6

Solving Radical Equations

HW 9-5

1. You can take the cube root of -27 followed by raising that answer to the fourth power making the answer 81.

2. $3x^2$

3. a. $x^{\frac{8}{15}}$ b. $3^{\frac{5}{12}}$

4. a. $\frac{1}{a^{\frac{1}{3}}}$ or $\frac{1}{\sqrt[3]{a}}$ b. $\frac{1}{b^{\frac{1}{16}}}$ or $\frac{1}{\sqrt[16]{b}}$ c. $\frac{1}{b^{\frac{1}{16}}}$ or $\frac{1}{\sqrt[16]{b}}$

5. -1 index 3 radicand -1

6. 3 index 4 radicand 81

7. $4a^2b^2\sqrt{2b}$

8. $2a^3b^4\sqrt[4]{3b^2}$

9. $3x^3$

10. $a^4\sqrt{7}$

11. $2b^3$

Name _____

Alg 2 HW 9-5

1. Explain how $(-27)^{\frac{4}{3}}$ can be evaluated using properties of rational exponents to result in an integer answer.

See explanation on first slide

2. Given the equal terms $\sqrt[5]{27x^6}$ and $y^{\frac{3}{5}}$, determine and state y , in terms of x . State your answer in simplest form.

$$\begin{aligned} \sqrt[5]{27x^6} &= y^{3/5} & (27x^6)^{1/3} &= y \\ (27x^6)^{1/5 \cdot 5/3} &= y^{3/5 \cdot 5/3} & y &= \sqrt[3]{27x^6} = 3x^2 \end{aligned}$$

3. Write as a single term with a rational exponent.

a. $\sqrt[5]{x} \cdot \sqrt[3]{x}$

$$x^{1/5} \cdot x^{1/3}$$

$$x^{3/15} \cdot x^{5/15}$$

$$x^{8/15}$$

b. $\sqrt[4]{3} \cdot \sqrt[6]{3}$

$$3^{1/4} \cdot 3^{1/6}$$

$$3^{3/12} \cdot 3^{2/12}$$

$$3^{5/12}$$

4. Using the rules for positive and negative exponents, simplify the following expressions.

a. $\left(\frac{a^{\frac{1}{3}}}{a^{\frac{1}{6}}}\right)^{-2}$

$$= \left(\frac{a^{\frac{1}{6}}}{a^{\frac{1}{3}}}\right)^2 = \frac{a^{\frac{2}{6}}}{a^{\frac{2}{3}}} = \frac{1}{a^{\frac{1}{3}}} \text{ or } \frac{1}{\sqrt[3]{a}}$$

b. $\left(\frac{b^2}{b^{\frac{9}{8}}}\right)^{-\frac{1}{2}} : \left(\frac{b^{\frac{9}{8}}}{b^2}\right)^{\frac{1}{2}}$

$$= \frac{b^{\frac{9}{16}}}{b^1} = \frac{1}{b^{\frac{7}{16}}} \text{ or } \frac{1}{\sqrt[16]{b^7}}$$

c. $\left(b^{\frac{7}{8}}\right)^{-\frac{1}{2}} = b^{-\frac{7}{16}}$

$$= \frac{1}{b^{\frac{7}{16}}} \text{ or } \frac{1}{\sqrt[16]{b^7}}$$

Simplify. Identify the index and the radicand.

5. $\sqrt[3]{-1}$

Answer -1

Index 3

Radicand -1

6. $\sqrt[4]{81}$

Answer 3

Index 4

Radicand 81

Simplify.

$$\begin{aligned} 7. \sqrt{32a^4b^5} \\ &= \sqrt{16a^4b^4} \sqrt{2b} \\ &= 4a^2b^2\sqrt{2b} \end{aligned}$$

$$\begin{aligned} 8. \sqrt[4]{48a^{12}b^6} \\ &= \sqrt[4]{16a^{12}b^4} \sqrt[4]{3b^2} \\ &= 2a^3b\sqrt[4]{3b^2} \end{aligned}$$

$$9. \sqrt[3]{27x^9} = 3x^3$$

Divide and Simplify.

$$\begin{aligned} 10. \frac{\sqrt{14a^{13}}}{\sqrt{2a^5}} &= \sqrt{\frac{14a^{13}}{2a^5}} = \sqrt{7a^8} \\ &= a^4\sqrt{7} \end{aligned}$$

$$\begin{aligned} 11. \frac{\sqrt[4]{32b^{20}}}{\sqrt[4]{2b^8}} &= \sqrt[4]{\frac{32b^{20}}{2b^8}} \\ &= \sqrt[4]{16b^{12}} = 2b^3 \end{aligned}$$

Solving Radical Equations

Unit 9 Day 6

Warmup:

Express the fraction $\frac{2x^{\frac{3}{2}}}{(16x^4)^{\frac{1}{4}}}$ in simplest radical form.

$$\frac{2x^{\frac{3}{2}}}{\sqrt[4]{16x^4}} = \frac{2x^{\frac{3}{2}}}{2x^1} = x^{\frac{1}{2}} = \sqrt{x}$$

Solving Radical Equations

Unit 9 Day 6

Steps:

1. Isolate the expression containing the radical.
(Be sure to have only one radical per side.)
2. Square both sides.
3. Solve the resulting equation.
4. Must Check (extraneous roots!) !!!
→ check in the original equation
5. Write the solution set { }

Example:

$$(\sqrt{2x+1}-3)^2$$

$$2x+1=9$$

$$2x=8$$

$$x=4$$

$$\text{ck: } \sqrt{2(4)+1}=3$$

$$\sqrt{9}=3$$

$$3=3 \checkmark$$

Solve and check.

$$1. (\sqrt{x^2+7})^2 = (x+1)^2 \quad \text{Double Dist!}$$

$$x^2+7 = x^2+2x+1$$

$$7 = 2x+1$$

$$6 = 2x$$

$$3 = x$$

$$\text{ck: } \sqrt{3^2+7} = 3+1$$

$$\sqrt{16} = 4$$

$$4 = 4 \checkmark$$

$$\{3\}$$

$$2. \sqrt{x+7}-1=x$$

$$(\sqrt{x+7})^2 = (x+1)^2 \quad \text{Double Dist!}$$

$$x+7 = x^2+2x+1$$

$$0 = x^2+x-6$$

$$0 = (x+3)(x-2)$$

$$x = -3$$

$$x = 2$$

$$\text{ck: } \sqrt{-3+7}-1 = -3$$

$$\sqrt{4}-1 = -3$$

$$2-1 = -3$$

$$1 \neq -3$$

$$\text{ck: } \sqrt{2+7}-1 = 2$$

$$\sqrt{9}-1 = 2$$

$$3-1 = 2$$

$$2 = 2 \checkmark$$

$$\{2\}$$

$$(\sqrt{3x-4})^2 = (\sqrt{2x+3})^2$$

$$3x-4 = 2x+3$$

$$x = 7$$

$$\text{ck: } \frac{\sqrt{3(7)-4}}{\sqrt{17}} - \frac{\sqrt{2(7)+3}}{\sqrt{17}} = 0$$

$$0 = 0 \checkmark$$

$$\{7\}$$

$$4. \sqrt{3x+13} - 5 = x$$

$$(\sqrt{3x+13})^2 = (x+5)^2 \quad \text{Double Dist!} \quad (x+5)(x+5)$$

$$3x+13 = x^2+10x+25$$

$$0 = x^2+7x+12$$

$$0 = (x+4)(x+3)$$

$$x = -4 \quad x = -3$$

$$\begin{array}{l} \text{ck: } \sqrt{3(-4)+13} - 5 = -4 \\ \sqrt{1} - 5 = -4 \\ 1 - 5 = -4 \\ -4 = -4 \checkmark \end{array}$$

$$\begin{array}{l} \text{ck: } \sqrt{3(-3)+13} - 5 = -3 \\ \sqrt{4} - 5 = -3 \\ 2 - 5 = -3 \\ -3 = -3 \checkmark \end{array}$$

$$\{-4, -3\}$$

5. $\sqrt{2x+1} + x = 1$

$$(\sqrt{2x+1})^2 = (1-x)^2 \quad (1-x)(1-x)$$

$$2x+1 = 1-2x+x^2 \quad \leftarrow 1-x-x+x^2$$

$$0 = x^2 - 4x$$

$$0 = x(x-4)$$

$x=0$	$x=4$
ck $\sqrt{2(0)+1} + 0 = 1$	$\sqrt{2(4)+1} + 4 = 1$
$\sqrt{1} + 0 = 1$	$\sqrt{9} + 4 = 1$
$1 + 0 = 1$	$3 + 4 = 1$
$1 = 1$	$7 \neq 1$

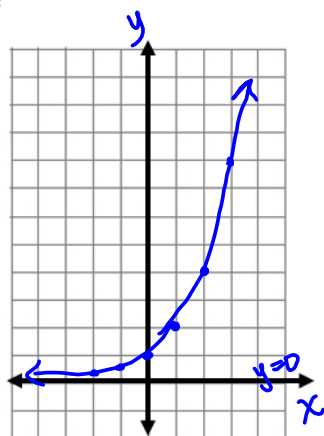
$\{0\}$

Exponential Growth & Decay

Unit 9 Day 7

Exponential Function: $f(x) = b^x$ Graph $f(x) = 2^x$

x	y
-2	$\frac{1}{4}$
-1	$\frac{1}{2}$
0	1
1	2
2	4

Exponential growth or decay?

(Circle One)

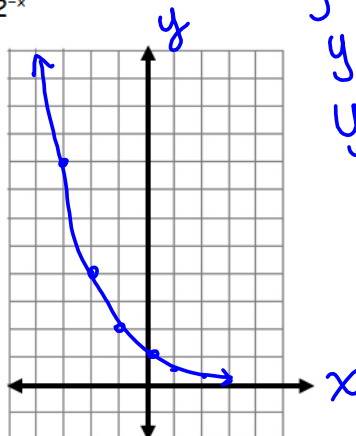
End Behavior:

$x \rightarrow -\infty, f(x) \rightarrow \underline{0}$

$x \rightarrow \infty, f(x) \rightarrow \underline{\infty}$

Graph $f(x) = 2^{-x}$

x	y
-2	4
-1	2
0	1
1	$\frac{1}{2}$
2	$\frac{1}{4}$

Exponential growth or decay?

(Circle One)

End Behavior:

$x \rightarrow -\infty, f(x) \rightarrow \underline{\infty}$

$x \rightarrow \infty, f(x) \rightarrow \underline{0}$

$$y = 2^{-x}$$

$$y = (2^{-1})^x$$

$$y = \left(\frac{1}{2}\right)^x$$

How can you tell from a given exponential function whether or not it will grow or decay?

look at Base.

if base > 1 growth
 base < 1 decay

Summary:

Point on every exponential graph: $(0, 1)$

Domain: $(-\infty, \infty)$

Range: $(0, \infty)$

Quadrants: I, II

Asymptote(s)? $x\text{-axis } (y=0)$

Are exponential functions 1-1? How can you tell? What does this tell you about their inverses?
