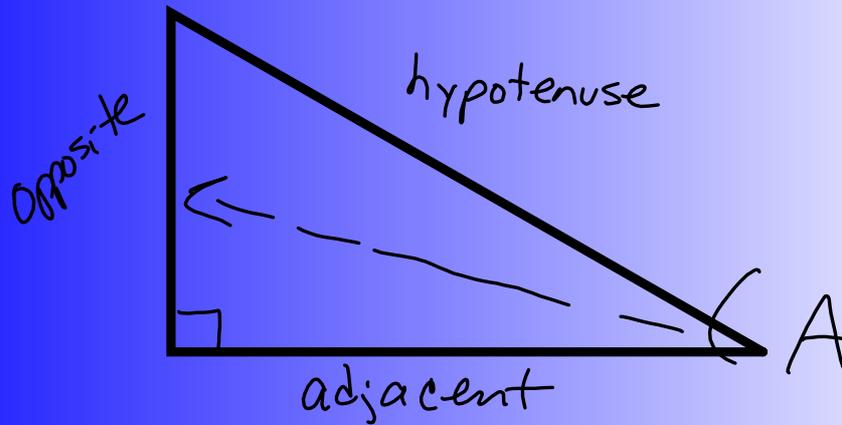


# Day 1: Right Triangles



Aug 8-8:59 PM

$$\sin(A) = \frac{\text{opposite}}{\text{hypotenuse}}$$

$$\cos(A) = \frac{\text{adjacent}}{\text{hypotenuse}}$$

$$\tan(A) = \frac{\text{opposite}}{\text{adjacent}}$$

Pythagorean Theorem

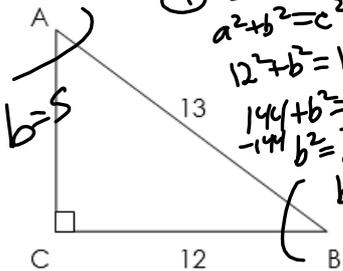
$$a^2 + b^2 = c^2$$

leg<sup>2</sup> leg<sup>2</sup> hypotenuse<sup>2</sup>

**S**in **A** = **O**pposite / **H**ypotenuse  
**C**os **A** = **A**djacent / **H**ypotenuse  
**T**an **A** = **O**pposite / **A**djacent

What mnemonic do you use?

Pythag. Triple: 5, 12, 13



①  $b =$   
 $a^2 + b^2 = c^2$   
 $12^2 + b^2 = 13^2$   
 $144 + b^2 = 169$   
 $-144 \quad -144$   
 $b^2 = 25$   
 $b = 5$

$$\sin(A) = \frac{5}{13} = \frac{12}{13}$$

$$\sin(B) = \frac{12}{13} = \frac{5}{13}$$

$$\cos(A) = \frac{12}{13} = \frac{5}{13}$$

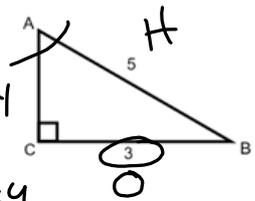
$$\cos(B) = \frac{5}{13} = \frac{12}{13}$$

$$\tan(A) = \frac{5}{12} = \frac{12}{5}$$

$$\tan(B) = \frac{12}{5} = \frac{5}{12}$$

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1. Find  $\sin(A)$ ,  $\cos(A)$ ,  $\tan(A)$  and  $m\angle A$  to nearest degree.

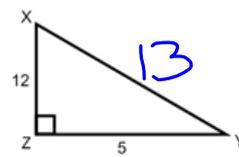


$\sin A = \frac{3}{5}$   
 $\cos A = \frac{4}{5}$   
 $\tan A = \frac{3}{4}$

$m\angle A = \sin^{-1}(3/5) = 36.9^\circ \approx 37^\circ$

Calc: Degree mode

2. Find  $\cos(X)$ ,  $\sin(X)$ ,  $\tan(Y)$  and  $m\angle X$  to nearest degree.



$\cos(X) = \frac{12}{13}$   
 $\sin(X) = \frac{5}{13}$   
 $\tan(Y) = \frac{12}{5}$

$m\angle X = \cos^{-1}(12/13) = 23^\circ$

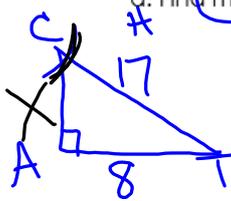
$a^2 + b^2 = c^2$   
 $3^2 + 4^2 = 5^2$   
 $9 + 16 = 25$   
 $b^2 = 16$   
 $b = 4$

Pythagorean Triple  
3-4-5

$a^2 + b^2 = c^2$   
 $5^2 + 12^2 = c^2$   
 $25 + 144 = c^2$   
 $\sqrt{169} = \sqrt{c^2}$   
 $c = 13$

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3. Given  $\triangle CAT$  with hypotenuse  $CT$ . The side opposite  $\angle C$  is 8 units long and the hypotenuse is 17 units long.



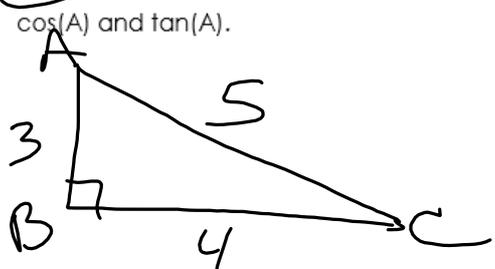
a. Find  $m\angle C$  to nearest degree

$\sin C = \frac{8}{17}$   
 $m\angle C = \sin^{-1}(8/17)$   
 $m\angle C = 28^\circ$

b. Use  $m\angle C$  to find side  $CA$

$\cos 28^\circ = \frac{CA}{17}$   
 $CA = 17 \cos 28^\circ = 15.0101 \approx 15$

4. Sketch triangle  $ABC$ , where angle  $B$  is the right angle and  $\sin(A) = \frac{4}{5}$ . Then find  $\cos(A)$  and  $\tan(A)$ .



$\cos(A) = \frac{3}{5}$   
 $\tan(A) = \frac{4}{3}$

Pythagorean Triple  
3-4-5  
5-12-13  
8-15-17

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### Angle of Rotations/Quadrants

Parts of an angle:

Standard Position: The initial side of the angle is on the (+) x-axis

$\theta$  = Greek letter "theta" (a variable commonly used for angles)

Measures of  $\angle \theta$  in:

- Quad I  $0^\circ < \theta < 90^\circ$
- Quad II  $90^\circ < \theta < 180^\circ$
- Quad III  $180^\circ < \theta < 270^\circ$
- Quad IV  $270^\circ < \theta < 360^\circ$

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### Degree Measure

Positive angle: Counter clockwise direction

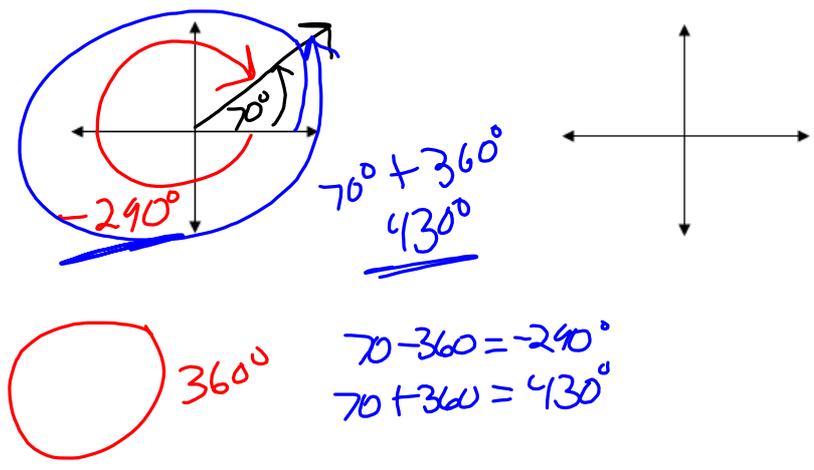
Negative angle: clockwise direction

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Day 2 - Co-Terminal Angles, Quadrantals and the Unit Circle

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Co-terminal Angles: angles that share the same initial and terminal sides  
 To find positive and negative co-terminal angles, add and subtract  $360^\circ$  to/from the angle. For example, two of the co-terminal angles for  $70^\circ$  are:



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