

Homework Answers pg 683 - 684:

17. (5, 4)

24. (-2, 3)

25. (1, -1)

27. $\left(\frac{1}{2}, \frac{3}{4}\right)$

32. (3, -1) consistent and independent

34. ~~no solution~~, inconsistent and independent

36. (3, 1) consistent and independent

39. (10, 8) consistent and independent

Extra Question: (-1, 2, 4)

Mar 8-9:31 AM

$$\begin{array}{l}
 25) \quad 2x - 3y = 5 \\
 \quad \quad 5x + 4y = 1
 \end{array}
 \quad
 \begin{array}{l}
 \frac{2x}{2} = \frac{3y}{2} + \frac{5}{2} \\
 x = \frac{3}{2}y + \frac{5}{2}
 \end{array}$$

$$5\left(\frac{3}{2}y + \frac{5}{2}\right) + 4y = 1$$

$$\frac{15}{2}y + \frac{25}{2} + \frac{8}{2}y = 1$$

$$\frac{23}{2}y = \frac{2}{2} - \frac{25}{2}$$

$$\frac{2}{23}\left(\frac{23}{2}y\right) = \left(\frac{-23}{2}\right)\frac{2}{23}$$

$$\underline{y = -1}$$

$$2x - 3y = 5$$

$$2x - 3(-1) = 5$$

$$2x + 3 = 5$$

$$2x = 2$$

$$x = 1$$

$$(1, -1)$$

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$$27) \begin{cases} x + 2y = 2 \\ 4x + 4y = 5 \end{cases} \rightarrow x = 2 - 2y$$

$$\underline{4x + 4y = 5}$$

$$4(2 - 2y) + 4y = 5$$

$$8 - 8y + 4y = 5$$

$$8 - 4y = 5$$

$$\underline{-4y = -3}$$

$$y = \frac{3}{4}$$

$$4x + 4\left(\frac{3}{4}\right) = 5$$

$$4x + 3 = 5$$

$$\underline{4x = 2}$$

$$x = \frac{1}{2}$$

$$4x = 2$$

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$$39) \begin{cases} \frac{1}{5}x + \frac{1}{2}y = 6 \\ \frac{3}{5}x - \frac{1}{2}y = 2 \end{cases} \cdot 10$$

$$\underline{\begin{cases} 2x + 5y = 60 \\ 6x - 5y = 20 \end{cases}}$$

$$2x + 5y = 60$$

$$6x - 5y = 20$$

$$\underline{8x = 80}$$

$$x = 10$$

$$\frac{1}{5}(10) + \frac{1}{2}(y) = 6$$

$$2 + \frac{1}{2}y = 6$$

$$2\left(\frac{1}{2}y\right) = (4)2$$

$$y = 8$$

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$$\begin{array}{l}
 \textcircled{1} \quad 3x - 2y + z = -3 \\
 \textcircled{2} \quad -x + y - 2z = -5 \\
 \textcircled{3} \quad x + y + z = 5
 \end{array}$$

$\underline{S+1: (1) + 3(2)}$

$$\begin{array}{r}
 3x - 2y + z = -3 \\
 -3x + 3y - 6z = -15 \\
 \hline
 y - 5z = -18
 \end{array}$$

$\underline{S+2: (1) + 3(3)}$

$$\begin{array}{r}
 3x - 2y + z = -3 \\
 -3x - 3y - 3z = 15 \\
 \hline
 -5y - 2z = 18
 \end{array}$$

$\underline{S+3: (y - 5z = -18) \times 5}$

$$\begin{array}{r}
 5y - 25z = -90 \\
 -5y - 2z = 18 \\
 \hline
 -27z = -108 \\
 \underline{-27} \quad \quad \quad z = 4
 \end{array}$$

$\underline{y}$

$$\begin{array}{r}
 y - 5(4) = -18 \\
 y - 20 = -18 \\
 \hline
 y = 2
 \end{array}$$

$x: x + 2 + 4 = 5$
 $x = -1$
 $(-1, 2, 4)$

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What are they used for?

Any data that is organized in columns and rows can be represented as a matrix. Matrices are used to represent real-world data such as the habits, or traits, of a population of people.

Matrix: An array of numbers named by the order or dimension, which is the number of rows by the number of columns. $\rightarrow$ elements

2 x 3 Matrix: $\begin{bmatrix} a & b & c \\ d & e & f \end{bmatrix}$

3 x 2 Matrix: $\begin{bmatrix} a & b \\ c & d \\ e & f \end{bmatrix}$

1 x 4 Matrix: $[a \ b \ c \ d]$

4 x 1 Matrix: $\begin{bmatrix} a \\ b \\ c \\ d \end{bmatrix}$

Square Matrix: Same number of rows and columns.
2x2, 3x3

or $\begin{pmatrix} 2 & 1 \\ 3 & 6 \\ 4 & 1 \end{pmatrix}$

or $\begin{bmatrix} \end{bmatrix}$ brackets

or $(\)$ parenthesis

Matrices are congruent if they have the same dimensions and are identical.

Find x and y.

1. $\begin{bmatrix} y-3 \\ y \end{bmatrix} = \begin{bmatrix} x \\ 2x \end{bmatrix}$

$y-3 = x$
 $y = 2x$

Subst. $2x-3 = x$ $y = 2(3)$
 $x = 3$ $y = 6$
 $\therefore (3, 6)$

2. $\begin{bmatrix} y+4 & 3 \\ y & -1 \end{bmatrix} = \begin{bmatrix} x-1 & 3 \\ 3x & -1 \end{bmatrix}$

$y+4 = x-1$ $\therefore (-5, -15)$
 $y = 3x$

$3x+4 = x-1$ $y = 3(-5/2)$
 $2x = -5$ $y = -15/2$
 $x = -5/2$

Matrices with the same order or dimensions can be added or subtracted: add/subtract the elements in the same position together.

Find $A+B$, $A-B$, and $D-C$:

$$A = \begin{bmatrix} 1 & -3 \\ 4 & 6 \end{bmatrix} \quad B = \begin{bmatrix} -5 & 3 \\ 2 & 1 \end{bmatrix} \quad C = \begin{bmatrix} -2 & -9 & 0 \\ 1 & 3 & 1 \\ -1/2 & 2 & 1/3 \end{bmatrix} \quad D = \begin{bmatrix} -3 & 0 & 2 \\ 1/2 & 1 & 4 \\ -1 & 3 & 0 \end{bmatrix}$$

$$\begin{aligned} A+B &= \begin{bmatrix} 1-5 & -3+3 \\ 4+2 & 6+1 \end{bmatrix} = \begin{bmatrix} -4 & 0 \\ 6 & 7 \end{bmatrix} & A-B &= \begin{bmatrix} 1+5 & -3-3 \\ 4-2 & 6-1 \end{bmatrix} = \begin{bmatrix} 6 & -6 \\ 2 & 5 \end{bmatrix} & D-C &= \begin{bmatrix} -3+2 & 0+9 & 2-0 \\ 1/2-1 & 1-3 & 4-1 \\ -1+1/2 & 3-2 & 0-1/3 \end{bmatrix} = \begin{bmatrix} -1 & 9 & 2 \\ -1/2 & -2 & 3 \\ -1/2 & 1 & -1/3 \end{bmatrix} \end{aligned}$$

Multiplication of Matrices:

Scalar Multiplication: $2 \begin{bmatrix} a & b \\ c & d \end{bmatrix} = \begin{bmatrix} 2a & 2b \\ 2c & 2d \end{bmatrix}$

Multiply: $3 \begin{bmatrix} -2 & -1 \\ 0 & 5 \end{bmatrix} = \begin{bmatrix} -6 & -3 \\ 0 & 15 \end{bmatrix}$

Matrix Multiplication: $\begin{bmatrix} a & b \\ c & d \end{bmatrix} \cdot \begin{bmatrix} x_1 & w \\ y_1 & z \end{bmatrix} = \begin{bmatrix} ax+by & aw+bz \\ cx+dy & cw+dz \end{bmatrix}$

row $\times$ column

Matrices A & B can be multiplied only if the number of columns in A equals the number of rows in B.

Algebraically: The product of an $m \times n$ matrix and an $n \times p$ matrix is an $m \times p$ matrix.

Numerically: The product of a 2×3 matrix and a 3×4 matrix is a 2×4 matrix.

$(m \times n)(n \times p) = m \times p$

$2 \times 3 \text{ m} \times 3 \times 4 \text{ m}$
 $= 2 \times 4$
 $2 \times 3 \cdot 3 \times 4$
 $= 2 \times 4$

Given:

$A = \begin{bmatrix} -1 & 0 \\ 2 & 3 \end{bmatrix}$ $B = \begin{bmatrix} 1 & 4 \\ -1 & -2 \end{bmatrix}$ $C = \begin{bmatrix} -2 & 1 & 0 \end{bmatrix}$ $D = \begin{bmatrix} 5 \\ -2 \\ -1 \end{bmatrix}$

$E = \begin{bmatrix} -2 & 4 & 5 \\ 1 & 0 & 6 \end{bmatrix}$ $F = \begin{bmatrix} 1 & 2 \\ 0 & 2 \\ -1 & -2 \end{bmatrix}$ $G = \begin{bmatrix} 0 & 1 \\ 1 & -2 \end{bmatrix}$

Find:

1. AB
2. BA

$\neq []$ matrix multiplication is not commutative.

$$A = \begin{bmatrix} -1 & 0 \\ 2 & 3 \end{bmatrix}_{2 \times 2} \cdot \begin{bmatrix} 1 & 4 \\ -1 & -2 \end{bmatrix}_{2 \times 2} = 2 \times 2$$

$$= \begin{bmatrix} \frac{-1(1)+0(-1)}{2(1)+3(-1)} & \frac{-1(4)+0(-2)}{2(4)+3(-2)} \\ \frac{-1(1)+0(-1)}{2(1)+3(-1)} & \frac{-1(4)+0(-2)}{2(4)+3(-2)} \end{bmatrix}$$

$$= \begin{bmatrix} -1 & -4 \\ -1 & 2 \end{bmatrix}$$

$$B = \begin{bmatrix} 1 & 4 \\ -1 & -2 \end{bmatrix} \quad A = \begin{bmatrix} -1 & 0 \\ 2 & 3 \end{bmatrix} = \begin{bmatrix} \frac{1(-1) + 4(2)}{-1(-1) + -2(2)} & \frac{1(0) + 4(3)}{-1(0) + -2(3)} \end{bmatrix}$$

$$= \begin{bmatrix} 7 & 12 \\ -3 & -6 \end{bmatrix}$$

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Given:

$$A = \begin{bmatrix} -1 & 0 \\ 2 & 3 \end{bmatrix} \quad B = \begin{bmatrix} 1 & 4 \\ -1 & -2 \end{bmatrix} \quad C = \begin{bmatrix} -2 & 1 & 0 \end{bmatrix} \quad D = \begin{bmatrix} 5 \\ -2 \\ -1 \end{bmatrix}$$

$$E = \begin{bmatrix} -2 & 4 & 5 \\ 1 & 0 & 6 \end{bmatrix} \quad F = \begin{bmatrix} 1 & 2 \\ 0 & 2 \\ -1 & -2 \end{bmatrix} \quad G = \begin{bmatrix} 0 & 1 \\ 1 & -2 \end{bmatrix}$$

3. CD
4. EFG
5. 2FE

$$C = \begin{bmatrix} -2 & 1 & 0 \end{bmatrix}_{1 \times 3} \quad D = \begin{bmatrix} 5 \\ -2 \\ -1 \end{bmatrix}_{3 \times 1} = 1 \times 1$$

$$= \begin{bmatrix} -2(5) + 1(-2) + 0(-1) \end{bmatrix} = \begin{bmatrix} -10 - 2 + 0 \end{bmatrix}$$

$$= \begin{bmatrix} -12 \end{bmatrix}$$

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$$E = \begin{bmatrix} -2 & 4 & 5 \\ 1 & 0 & 6 \end{bmatrix}_{2 \times 3} \quad F = \begin{bmatrix} 1 & 2 \\ 0 & 2 \\ -1 & -2 \end{bmatrix}_{3 \times 2} \quad G = \begin{bmatrix} 0 & 1 \\ 1 & -2 \end{bmatrix}_{2 \times 2}$$

$E \cdot F = 2 \times 2$

$$EF = \begin{bmatrix} \frac{-2(1) + 4(0) + 5(-1)}{1(1) + 0(0) + 6(-1)} & \frac{-2(2) + 4(2) + 5(-2)}{1(2) + 0(2) + 6(-2)} \end{bmatrix} = \begin{bmatrix} -7 & -6 \\ -5 & -10 \end{bmatrix}$$

$(EF)G = 2 \times 2$

$$(EF)G = \begin{bmatrix} -7 & -6 \\ -5 & -10 \end{bmatrix}_{2 \times 2} \cdot \begin{bmatrix} 0 & 1 \\ 1 & -2 \end{bmatrix}_{2 \times 2} = \begin{bmatrix} \frac{-7(0) + -6(1)}{-5(0) + -10(1)} & \frac{-7(1) + -6(-2)}{-5(1) + -10(-2)} \end{bmatrix} = \begin{bmatrix} -6 & 5 \\ -10 & 15 \end{bmatrix}$$

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$$E = \begin{bmatrix} -2 & 4 & 5 \\ 1 & 0 & 6 \end{bmatrix} \quad F = \begin{bmatrix} 1 & 2 \\ 0 & 2 \\ -1 & -2 \end{bmatrix} \quad G = \begin{bmatrix} 0 & 1 \\ 1 & -2 \end{bmatrix}$$

$$EF = 2 \times 3 \times 3 \times 2 = \underline{2 \times 2}$$

$$(EF)G = 2 \times 2 \times 2 \times 2 = 2 \times 2$$

$$EF = \begin{bmatrix} \underline{-2(1)+4(0)+5(-1)} & \underline{-2(2)+4(2)+5(-2)} \\ \underline{1(1)+0(0)+6(-1)} & \underline{1(2)+0(2)+6(-2)} \end{bmatrix}$$

$$EF = \begin{bmatrix} -7 & -6 \\ -5 & -10 \end{bmatrix} \quad G = \begin{bmatrix} 0 & 1 \\ 1 & -2 \end{bmatrix}$$

$$(EF)G = \begin{bmatrix} \underline{-7(0)+-6(1)} & \underline{-7(1)+-6(-2)} \\ \underline{-5(0)+-10(1)} & \underline{-5(1)+-10(-2)} \end{bmatrix} = \begin{bmatrix} -6 & 5 \\ -10 & 15 \end{bmatrix}$$

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2 → $F = \begin{bmatrix} 1 & 2 \\ 0 & 2 \\ -1 & -2 \end{bmatrix} \quad E = \begin{bmatrix} -2 & 4 & 5 \\ 1 & 0 & 6 \end{bmatrix}$

$3 \times 2 \cdot 2 \times 3 = 3 \times 3$

$$\begin{bmatrix} _ & _ & _ \\ _ & _ & _ \\ _ & _ & _ \end{bmatrix}$$

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$$2 \quad F = \begin{bmatrix} 1 & 2 \\ 0 & 2 \\ -1 & -2 \end{bmatrix} \quad E = \begin{bmatrix} -2 & 4 & 5 \\ 1 & 0 & 6 \end{bmatrix} \quad \begin{matrix} 3 \times 2 & \times & 2 \times 3 \\ \hline & \checkmark & \\ & & \end{matrix} = 3 \times 3$$

$$2F = \begin{bmatrix} 2 & 4 \\ 0 & 4 \\ -2 & -4 \end{bmatrix} \quad E = \begin{bmatrix} -2 & 4 & 5 \\ 1 & 0 & 6 \end{bmatrix}$$

$$= \begin{bmatrix} \frac{2(-2)+4(1)}{0(-2)+4(1)} & \frac{2(4)+4(0)}{0(4)+4(0)} & \frac{2(5)+4(6)}{0(5)+4(6)} \\ -2(-2)+4(1) & -2(4)+4(0) & -2(5)+4(6) \end{bmatrix}$$

$$= \begin{bmatrix} 0 & 8 & 34 \\ 4 & 0 & 24 \\ 0 & -8 & -34 \end{bmatrix}$$

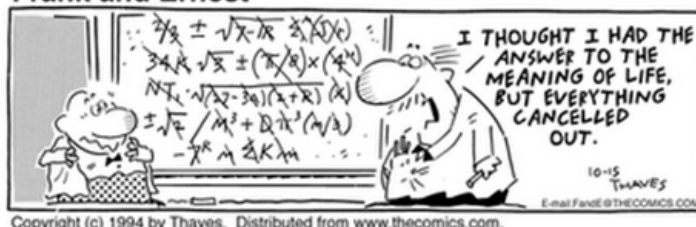
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Homework:

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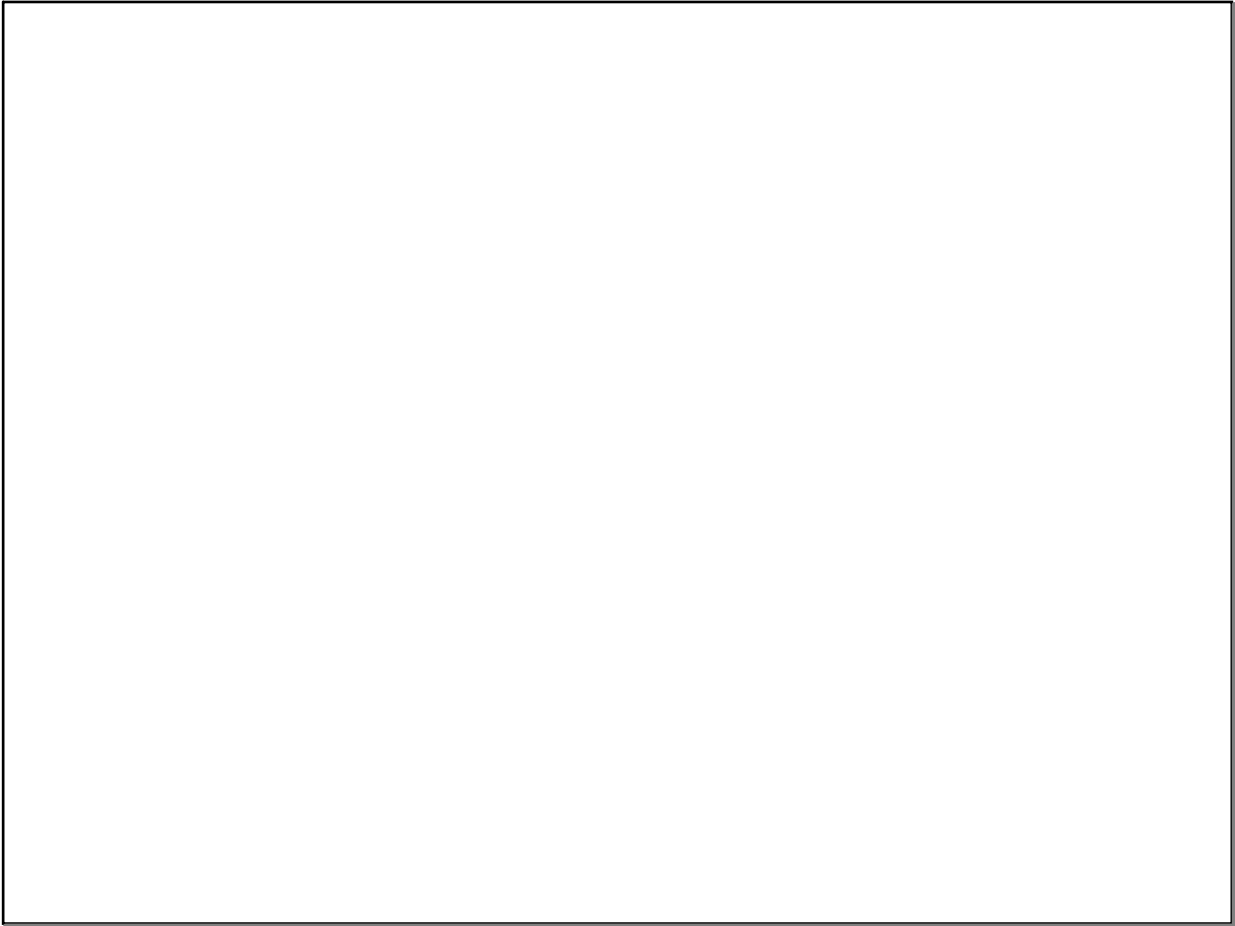
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Frank and Ernest



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