

Turn in your GrHW #5 with work stapled to the back

But we're starting with the notes

Theory of Equations



http://www.desktopscenes.com/Scenes%20from%20a%20Day%20at%20Yosemite%20(2003)Ribbon%20at%20Vernal%20Fall.jpg

pg 328:

23. $(-\infty, -2) \cup [2, \infty)$

32. $[-2, -1] \cup [2, \infty)$

51. $(2, \frac{7}{2}]$

52. $(-\infty, 5) \cup (10, \infty)$

54. $(-\infty, 0) \cup [2]$

Ditto 3.1

7. hole: $(5, \frac{1}{10})$

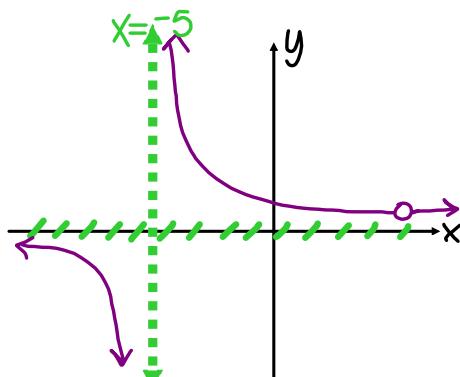
x-int: none

y-int: $(0, \frac{1}{5})$

VA: $x = -5$

HA: $y = 0$

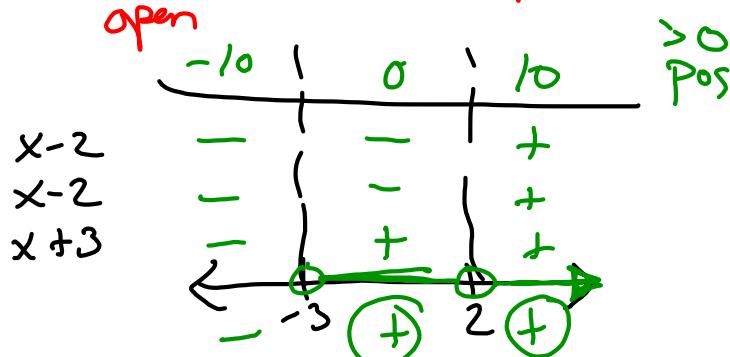
Cross? NO



Nov 6-8:50 AM

7. $\frac{x^2 - 4x + 4}{x+3} > 0$

$\text{num} = 0 \quad *$ $x^2 - 4x + 4 = 0$ $(x-2)(x-2) = 0$ $x=2 \quad \quad x=2$ open	$\text{den} = 0$ $x+3=0$ $x=-3$ open
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$$\{x \mid -3 < x < 2, x > 2\}$$

or $(-3, 2) \cup (2, \infty)$

Nov 1-10:10 AM

Warm-Up:

Find the y-intercept: $f(x) = 2(x+1)^2(x+2)^2(x-1)^3$

$$(0, -8)$$

$$f(0) = 2(0+1)^2(0+2)^2(0-1)^3$$

$$f(0) = -8$$

Oct 4-9:31 AM

Theory:

Degree of polynomial is the same as the number of complex roots.
All non-real complex roots must occur in pairs with their conjugate.

1. Write an equation of a polynomial whose roots include 2 and $2+i$.

$$\text{roots} = 2, 2+i, 2-i$$

$$\frac{x-2}{x-2}$$

$$\begin{aligned} \alpha &= 1 \\ b &= -\text{sum} = -(2+i + 2-i) = -4 = b \\ c &= \text{prod} = (2+i)(2-i) = 4-i^2 = 4+1 = 5 = c \end{aligned} \quad x^2 - 4x + 5 = 0$$

$$\begin{aligned} P(x) &= (x-2)(x^2 - 4x + 5) = 0 \\ P(x) &= x^3 - 4x^2 + 5x - 2x^2 + 8x - 10 \\ P(x) &= x^3 - 6x^2 + 13x - 10 \end{aligned}$$

But? $x^3 - 6x^2 + 13x - 10 = 0$

Oct 4-9:31 AM

2. Create a function that has a hole at $(1, -1/2)$ and vertical asymptotes at $x = 2$ and $x = 3$ and $x = -3$. $P(x) = \underline{\hspace{2cm}}$

$$\text{VA} \rightarrow \text{denom} = (x-2)(x-3)(x+3)$$

Hole $(1, -\frac{1}{2}) \rightarrow \frac{x-1}{x-1}$ $P(x) = \frac{K()}{()()()}$

$$f(1) = -\frac{1}{2} \quad K$$

$$\frac{-\frac{1}{2}}{(x-2)(x-3)(x+3)} = \frac{K}{(1-2)(1-3)(1+3)}$$

$$-\frac{1}{2} = \frac{K}{(-1)(-2)(4)}$$

$$-\frac{1}{2} \cancel{\times \frac{K}{8}} \quad -8 = 2K$$

$$K = -4$$

$$P(x) = \frac{-4(x-1)}{(x-1)(x-2)(x-3)(x+3)}$$

Oct 4-9:31 AM

3. Create a function that has a hole at $(2, -6)$ and vertical asymptotes at $x = 1$ and $x = -1$.

$$\text{VA} \rightarrow \text{denom} = (x-1)(x+1)$$

Hole $(2, -6) \rightarrow \frac{x-2}{x-2}$ $P(2) = -6$

Find K $-6 = \frac{K}{(x-1)(x+1)} \quad x=2$

$$-6 = \frac{K}{(2-1)(2+1)}$$

$$-6 = \frac{K}{(1)(3)}$$

$$\frac{-6}{1} = \frac{K}{3}$$

$$\underline{-18 = K}$$

$$P(x) = \frac{-18(x-2)}{(x-2)(x-1)(x+1)}$$

$$18 |c = -\frac{1}{18}$$

$$P(x) = \frac{(x-2)}{-18(x-2)(x-1)(x+1)}$$

Oct 4-9:31 AM

4. Create a function that has x-intercepts at $(-1, 0)$ and $(3, 0)$, vertical asymptotes at $x = 1$ and $x = 0$ and a horizontal asymptote at $y = 3$.

$$\text{VA} \rightarrow \text{den} = x(x-1)$$

$$x\text{-ints} \rightarrow \frac{0}{1} = \frac{0}{d}$$

$(-1, 0)$ $(3, 0)$

$$0 = n$$

$$0 = (x+1)(x-3)$$

num = \uparrow

$$\text{HA: } y = 3$$

$$\frac{(3)x^2}{1x^2}$$

$$k = 3$$

$$P(x) = \frac{3(x+1)(x-3)}{x(x-1)}$$

Oct 4-9:31 AM

Homework: pg 343 # 75; pg 345 #28

Write the Equation:

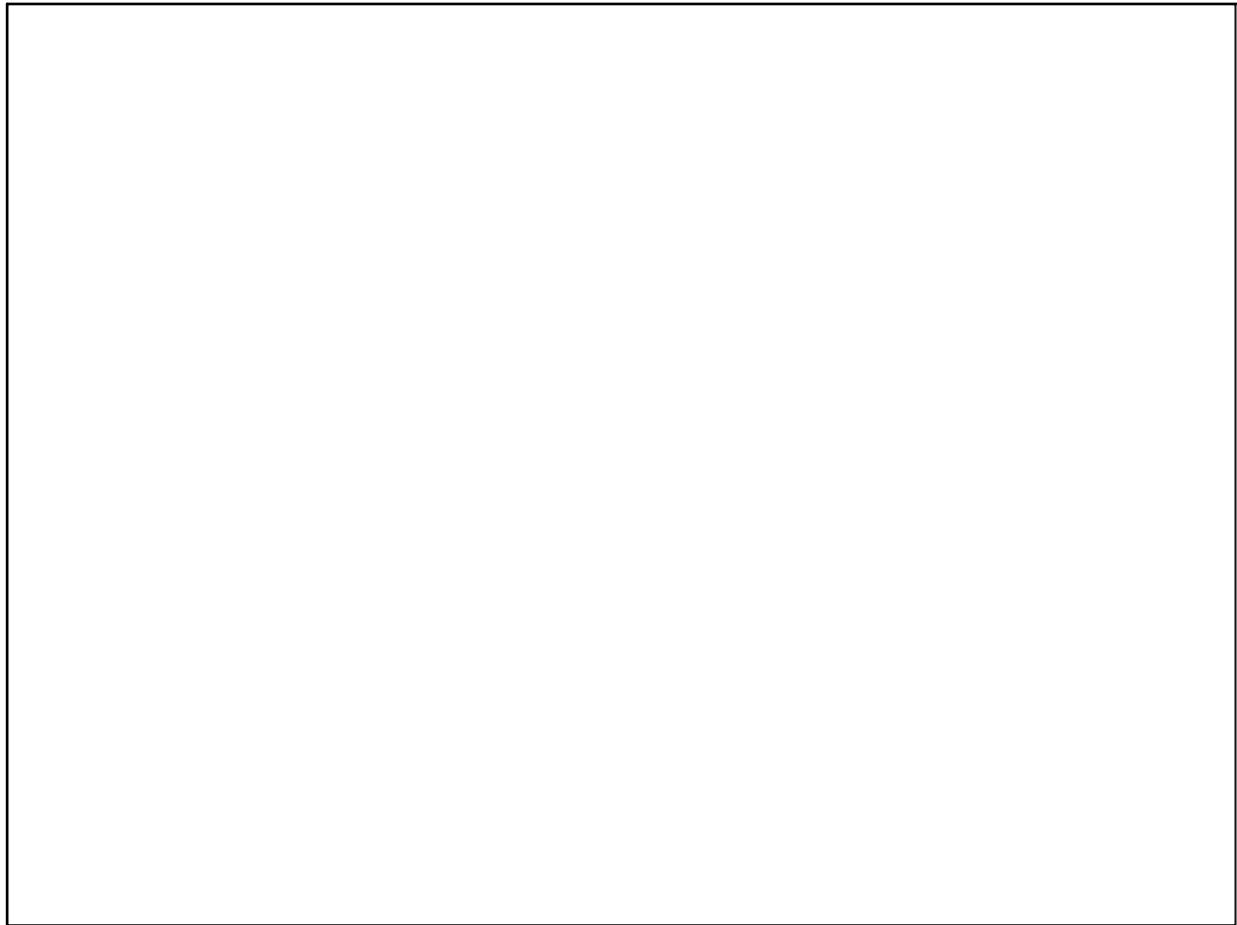
Test Tuesday!

1) Hole at $(-4, 2)$, va: $x = 1, x = -1$

2) Hole at $(3, 1/4)$, va: $x = 1$

3) x -intercepts: $(0, 0), (2, 0)$, va: $x = -3, x = 1$
 ha: $y = 2$

Nov 4-1:09 PM



Nov 5-9:01 AM