

Turn in Graded HW with work stapled to the back

QUIZ

You need your calculator for notes.

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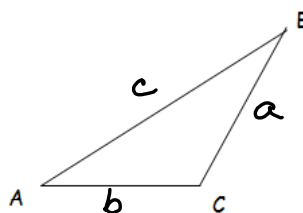
The Law of Cosines (SAS)

The Law of Cosines is commonly used to solve oblique triangles and forms the basis for important trigonometric applications. When two sides of a triangle and the included angle are known, the law of cosines can be used to find the third side.

Law of Cosines: $a^2 = b^2 + c^2 - 2bc \cos A$

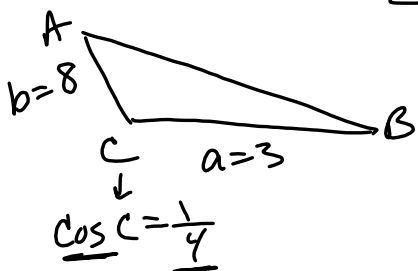
$$b^2 = a^2 + c^2 - 2ac \cos B$$

$$c^2 = a^2 + b^2 - 2ab \cos C$$



For each problem, draw a diagram and solve:

1. In $\triangle ABC$, $a = 3$, $b = 8$, and $\cos C = \frac{1}{4}$. Find c to the nearest integer.



$$c^2 = a^2 + b^2 - 2ab \cos C$$

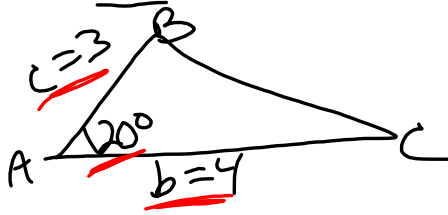
$$c^2 = 3^2 + 8^2 - 2(3)(8)\left(\frac{1}{4}\right)$$

$$\sqrt{c^2} = \sqrt{61}$$

$$c = \sqrt{61} = 7.8 \approx 8$$

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2. In $\triangle ABC$, $b = 4$, $c = 3$, $\angle A = 120^\circ$. Find a to the nearest integer.



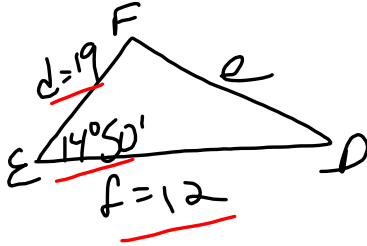
$$a^2 = b^2 + c^2 - 2bc \cos A$$

$$a^2 = 4^2 + 3^2 - 2(4)(3) \cos(120^\circ)$$

$$\sqrt{a^2} = \sqrt{37}$$

$$a \approx 6.08 \approx \textcircled{6}$$

3. In $\triangle DEF$, $f = 12$, $d = 19$, $\angle E = 14^\circ 50'$. Find e to the nearest integer.



$$e^2 = d^2 + f^2 - 2df \cos E$$

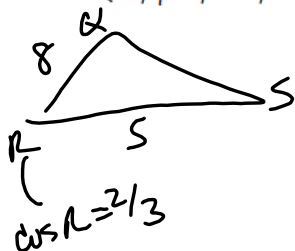
$$e^2 = 19^2 + 12^2 - 2(19)(12) \cos 14^\circ 50'$$

$$\sqrt{e^2} = \sqrt{64.19 \dots}$$

$$e \approx 8.012 \approx \textcircled{8}$$

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4. In $\triangle QRS$, $q = 5$, $s = 8$, and $\cos R = \frac{2}{3}$. Find r to the nearest integer.

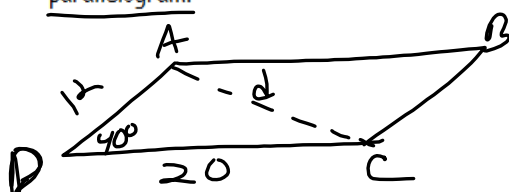


$$r^2 = 8^2 + 5^2 - 2(8)(5) \left(\frac{2}{3}\right)$$

$$r^2 = 35.6$$

$$r = 5.96 \approx \textcircled{6}$$

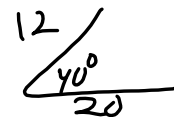
5. In a parallelogram, two sides that are 20 cm and 12 cm long include an angle of 40° . Find the length (to the nearest centimeter) of the shorter diagonal of the parallelogram.



$$d^2 = 12^2 + 20^2 - 2(12)(20) \cos 40^\circ$$

$$\sqrt{d^2} = \sqrt{176.2986}$$

$$d \approx 13.27 \approx \textcircled{13 \text{ cm}}$$



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The Law of Cosines (SSS) ←

$$c^2 = a^2 + b^2 - 2ab \cos C$$

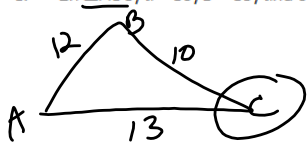
To find an angle of a triangle that does not contain a right angle where C is the angle opposite the side that you're looking for.

Draw a diagram and solve.

SSS

slide-slide
-divide

1. In $\triangle ABC$, $a = 10$, $b = 13$, and $c = 12$. Find $m\angle C$ to the nearest minute.



$$c^2 = a^2 + b^2 - 2ab \cos C$$

$$12^2 = 10^2 + 13^2 - 2(10)(13) \cos C$$

$$12^2 - 10^2 - 13^2 = -2(10)(13) \cos C$$

$$\cos C = \frac{(12^2 - 10^2 - 13^2)}{(-2(10)(13))}$$

$$\cos C = \frac{25}{52} \quad (.48076\dots)$$

$$m\angle C = \overset{(2nd \cos)}{\cos^{-1}}\left(\frac{25}{52}\right) = 61.26$$

2nd-Apps-1 →

$$DDms = 61^{\circ}15'51.647''$$

degrees ← minutes → seconds

51" (seconds is more than 1/2 a min)

$$m\angle C \approx 61^{\circ}16'$$

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