

Adv. Alg.-Trig.
Homework #8.1

Tonight's HW: Worksheet 8.2

1) $\tan^2 \theta$

2) $\cot^2 \theta$

3) $\cot \theta$

4) $\cos \theta$

5) $\sec \theta$

6) $\cos \theta$

7) $\cos^2 A$

8) $\frac{1}{\cos^2 C}$

9) $\frac{\sin R + \cos R}{\sin R \cos R}$

10) $\frac{\sin \theta \cos \theta - 1}{\sin \theta}$

4) $\frac{\sin \theta}{\tan} = (\cos \theta)$

$$\frac{\sin \theta}{\left(\frac{\sin \theta}{\cos \theta}\right)} = \frac{\sin \theta}{1} \cdot \frac{\cos \theta}{\sin \theta} = \cos \theta$$

5. $\tan \theta \cdot \csc \theta$

$$\frac{\sin \theta}{\cos \theta} \cdot \frac{1}{\sin \theta} = \frac{1}{\cos \theta} = \sec \theta$$

9. $\sec R + \csc R$

$$\frac{\sin \theta}{\sin \theta} \cdot \frac{1}{\cos \theta} + \frac{1}{\sin \theta} \cdot \frac{\cos \theta}{\cos \theta}$$

$$\frac{\sin \theta + \cos \theta}{\sin \theta \cos \theta}$$

Warm-Up

Simplify.

1) $(\sin \theta - \cos \theta)^2 \rightarrow \sin^2 \theta - 2\sin \theta \cos \theta + \cos^2 \theta$
 $1 - 2\sin \theta \cos \theta$

2) $\frac{1 - \sin^2 \theta}{\cot^2 \theta} = \frac{\cos^2 \theta}{1} \cdot \frac{\sin^2 \theta}{\cos^2 \theta} = \sin^2 \theta$

3) $\frac{\cot x}{\cos x}$

4) $\tan^2 x (1 + \cot^2 x)$

$$\boxed{\sin^2 \theta + \cos^2 \theta = 1}$$

$-\sin^2 \theta \quad -\sin^2 \theta$
 $\cos^2 \theta = 1 - \sin^2 \theta$

Quiz Yourself:

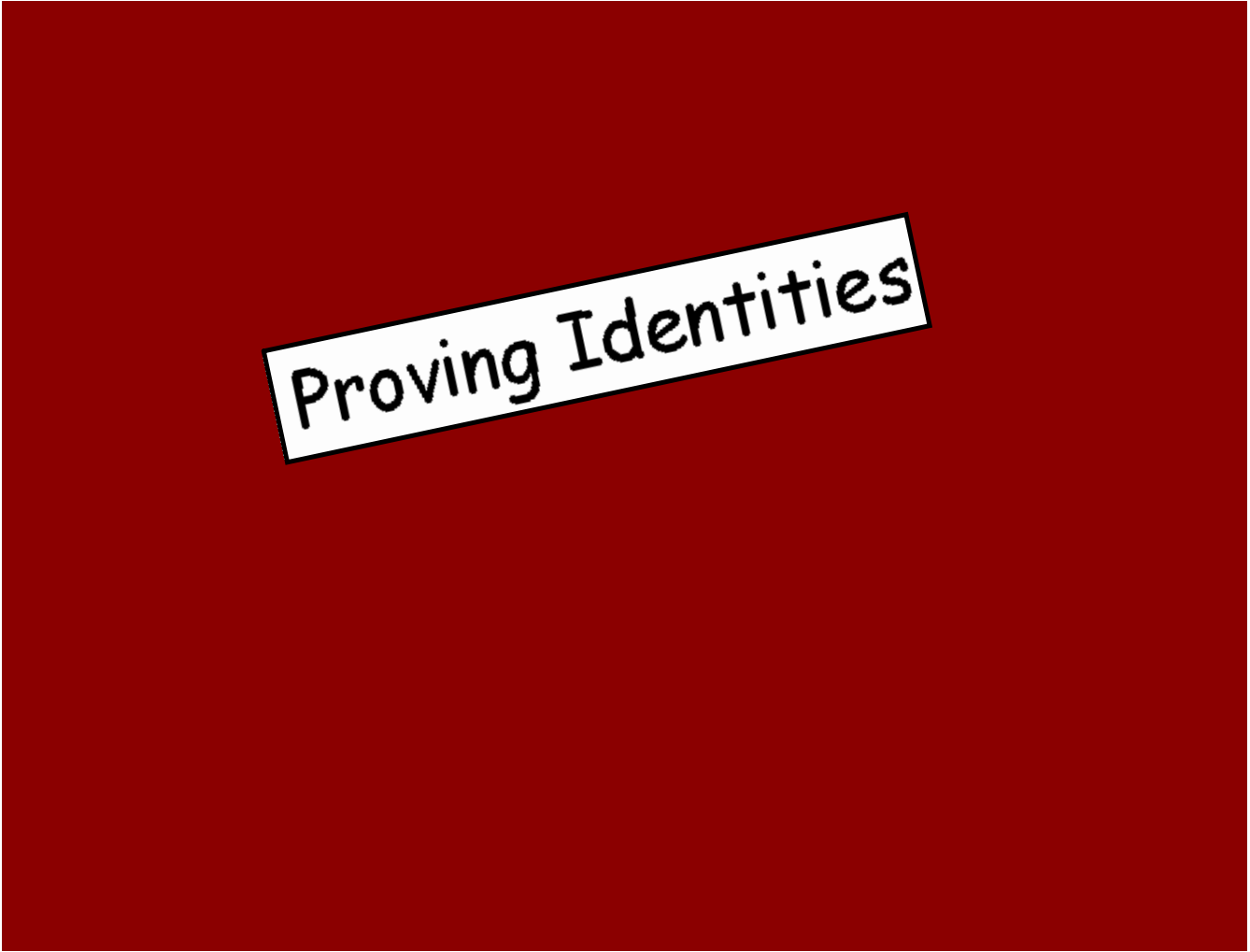
(1) $\sin^2 \theta + \underline{\hspace{2cm}} = 1$

(2) $\sin^2 \theta = \underline{\hspace{2cm}} - \underline{\hspace{2cm}}$

(3) $\cos^2 \theta = \underline{\hspace{2cm}} - \underline{\hspace{2cm}}$

(4) $\underline{\hspace{2cm}} + 1 = \sec^2 \theta$

(5) $\underline{\hspace{2cm}} + 1 = \csc^2 \theta$



Proving Identities

- Do not move terms from one side of the equation to the other.
- You may use identities on one (or) both sides of the equation.
- In general, start with the more complex side of the equation.
- Usually, put in terms of $\sin$ / $\cos$.

$$\begin{array}{l} 1) \tan x \csc x = \sec x \\ \frac{\sin x}{\cos x} \cdot \frac{1}{\sin x} = \frac{1}{\cos x} \\ \frac{1}{\cos x} = \frac{1}{\cos x} \\ \checkmark \end{array}$$

$$2) \cos^2 x = \csc x \sin x - \sin^2 x$$

$$1 - \sin^2 x \stackrel{?}{=} \frac{1}{\sin x} \cdot \frac{\sin x}{1} - \sin^2 x$$

$$1 - \sin^2 x \stackrel{?}{=} 1 - \sin^2 x$$

✓

Pyth id.

$$\begin{array}{l} \sin^2 x + \cos^2 x = 1 \\ -\sin^2 x \quad -\sin^2 x \\ \hline \cos^2 x = (1 - \sin^2 x) \end{array}$$

$$3) \tan^2 x + \sin^2 x + \cos^2 x = \sec^2 x$$

$$\frac{\sin^2 x}{\cos^2 x} \underbrace{\sin^2 x + \cos^2 x}_{=1} = \frac{1}{\cos^2 x}$$

$$\frac{\sin^2 x}{\cos^2 x} + \frac{1 \cdot \cos^2 x}{1 \cdot \cos^2 x} =$$

$$\frac{\sin^2 x + \cos^2 x}{\cos^2 x}$$

$$\frac{1}{\cos^2 x}$$

$$= \frac{1}{\cos^2 x}$$

$$4) (\sin x + \cos x)^2 = 1 + 2\sin x \cos x$$

$$\begin{aligned} & (\sin x + \cos x)(\sin x + \cos x) = \\ & \sin^2 x + 2\sin x \cos x + \cos^2 x = \\ & \underbrace{\sin^2 x + \cos^2 x}_{=1} + 2\sin x \cos x = 1 + 2\sin x \cos x \end{aligned}$$

$$5) \tan^2 A (1 + \cot^2 A) = \sec^2 A$$

$$\frac{\sin^2 A}{\cos^2 A} (\csc^2 A) =$$

$$\frac{\cancel{\sin^2 A}}{\cos^2 A} \left(\frac{1}{\cancel{\sin^2 A}} \right)$$

$$\frac{1}{\cos^2 A}$$

$$=$$

$$\frac{1}{\cos^2 A}$$

✓

Tonight's HW: Worksheet 8.2

wed: Quiz

