

Unit 9 - Law of Sines and Law of Cosines

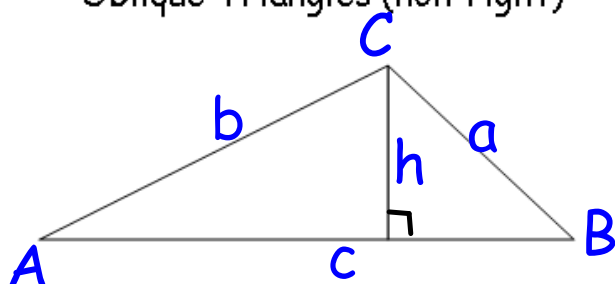
Test - Law of Sines

Quiz - Law of Cosines

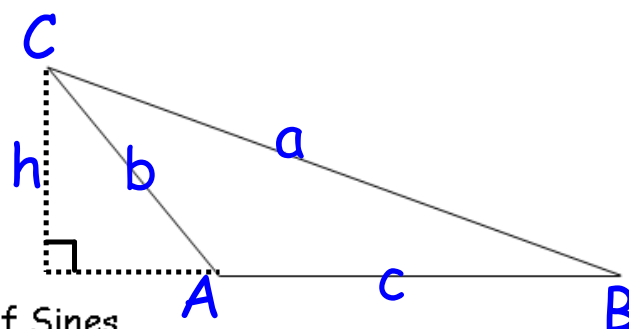
Test - Combined



Oblique Triangles (non-right)



Law of Sines



Law of Sines

In any triangle, the sines of the angles are proportional to the opposite sides.

$$\frac{\text{side } a}{\sin A} = \frac{\text{side } b}{\sin B} = \frac{\text{side } c}{\sin C}$$

Or

$$\frac{\sin A}{a} = \frac{\sin B}{b} = \frac{\sin C}{c}$$

Adv. Alg.-Trig.
Homework #9.1

1) 20

3) $a = 16$, $b = 16\sqrt{3}$ (27.7)

5) 61

7) 24ft

HW 9.2

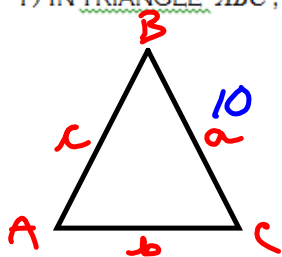
*Test on Law of Sines
Next Wednesday!*

2) $\frac{5}{6}$

4) $a = 66$, $c = 79$

6) 54

1) IN TRIANGLE ABC , $a = 10$, $\sin A = .30$, AND $\sin B = \frac{3}{5}$. FIND b .



$$\frac{a}{\sin A} = \frac{b}{\sin B}$$

$$\frac{10}{.30} = \frac{b}{3/5}$$

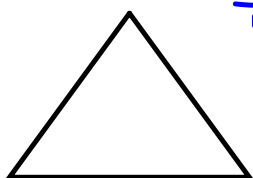
$$10 \cdot \frac{3}{3} = .30b$$

$$6 = .30b$$

$$\frac{6}{.30} = \frac{.30b}{.30}$$

$$b = 20$$

2) IN TRIANGLE ABC , $a = 6$, $\sin A = \frac{1}{4}$, AND $b = 20$. FIND $\sin B$.



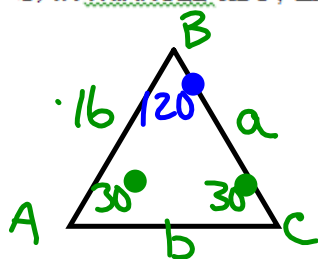
$$\frac{a}{\sin A} = \frac{b}{\sin B}$$

$$\frac{6}{1/4} = \frac{20}{\sin B}$$

$$6 \sin B = 5$$

$$\sin B = \frac{5}{6}$$

3) IN TRIANGLE ABC , $\angle A = 30^\circ$, $\angle C = 30^\circ$, AND $c = 16$. FIND a AND b .



$$\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$$

$$\frac{16}{\sin 30} = \frac{a}{\sin 30}$$

$$\frac{a \sin 30}{\sin 30} = \frac{16 \sin 30}{\sin 30}$$

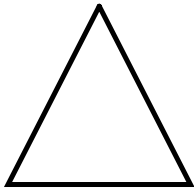
$$a = 16$$

$$\frac{b}{\sin 120} = \frac{16}{\sin 30}$$

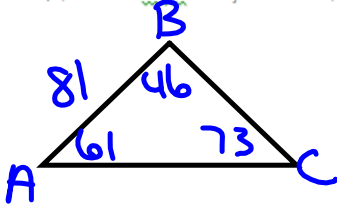
$$b = \frac{16 \cdot \sin 120}{\sin 30}$$

$$b = 27.7$$

4) IN TRIANGLE ABC , $\angle A = 48^\circ$, $\angle C = 62^\circ$, AND $b = 84$ feet. FIND a AND c TO THE NEAREST FOOT.



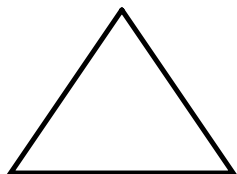
5) IN TRIANGLE ABC , $AB = 81$ feet, $\angle A = 61^\circ$, AND $\angle C = 73^\circ$. FIND THE LENGTH OF AC , CORRECT TO THE NEAREST FOOT.



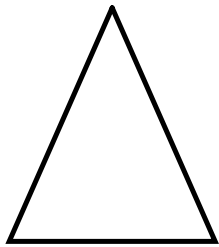
$$\frac{AC}{\sin 46} = \frac{81}{\sin 73}$$

$$AC = 61$$

6) IN TRIANGLE ABC , $AB = 50$, $\angle A = 71^\circ$, AND $\angle C = 49^\circ$. FIND THE LENGTH OF THE ALTITUDE ON AB , CORRECT TO THE NEAREST INTEGER.

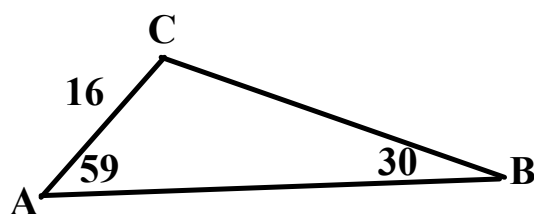


7) Two angles of a triangle are 25° and 70° and the longest side is 56 feet. Find the shortest side, correct to the nearest foot.

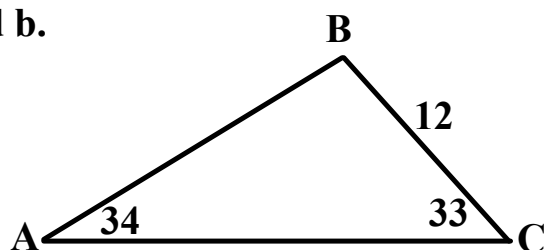


Warm-Up

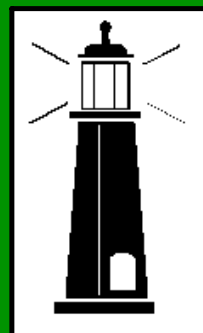
1) Find a.



2) Find b.



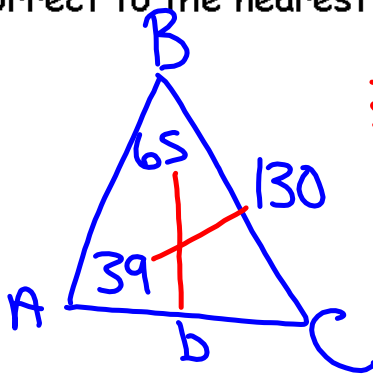
Law of Sines Word Problems



Law of Sines Word Problems

Problem #1

In Triangle ABC, $a = 130$ feet, angle $A = 39^\circ$, angle $B = 65^\circ$. Find side b , correct to the nearest 10 feet.



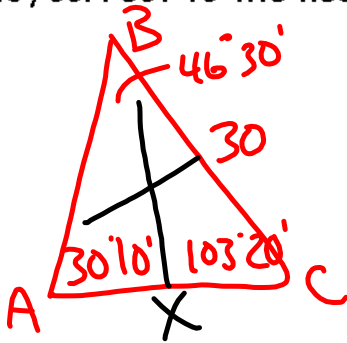
$$\frac{b}{\sin 65} = \frac{130}{\sin 39}$$

$$b = 187.2$$

$$b = 190 \text{ ft.}$$

Problem #2

In Triangle ABC, BC = 30 feet, angle A = $30^{\circ}10'$, and angle C = $103^{\circ}20'$. Find AC, correct to the nearest foot.



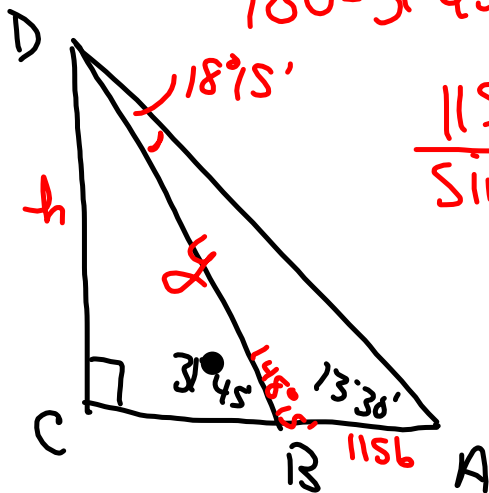
$$\frac{30}{\sin 30^{\circ}10'} = \frac{AC}{\sin 46^{\circ}30'}$$

$$AC = 43.3$$

$$AC = 43 \text{ ft}$$

Problem #3

A Lighthouse DC is sighted from two points, A and B, directly west of the lighthouse and on the same horizontal plane with its base C. At point A, the angle of elevation of D, the top of the lighthouse, is $13^\circ 30'$ and at point B the angle is $31^\circ 45'$. If AB is 1156 feet, find the height of the lighthouse to the nearest foot.



$$180^\circ - 31^\circ 45' = 148^\circ 15'$$

$$\frac{1156}{\sin 18^\circ 15'} = \frac{h}{\sin 13^\circ 30'}$$

finish Fri.

HW 9.2

*Test on Law of Sines
Next Wednesday!*

