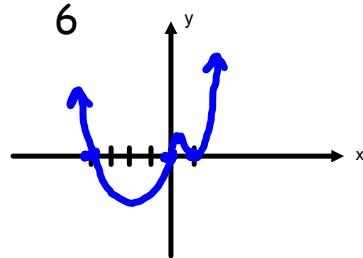


P. 270

- 12) a      14) c      16) b      18) d

22) 1, -2 are roots, 3 is not a root

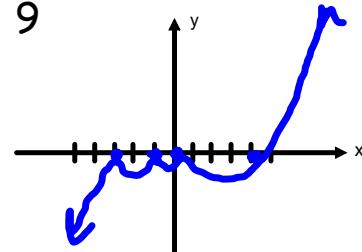
R	M	T/C
0	3	C
1	2	T
-4	1	C

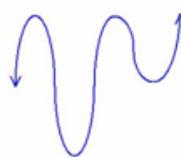


$$2x + x^3 - x^5$$

Odd nro

R	M	T/C
0	2	T
-3	2	T
4	1	C
-1	4	T





Steps:

1. determine end behavior
2. find zeros & multiplicity  
(determine if tangent or cross)
3. find a point in each region → between zeros
4. find y-intercept let  $x=0$  solve for y
5. sketch

yesterday

between zeros

For each problem:

- degree ←  
Same ←  
1 less ←
1. Determine
    - a. maximum # of real zeros
    - b. maximum # of x-intercepts
    - c. maximum # of turning points

} that the graph of the function can have
  2. Graph using the steps outlined above.

## Graphing Polynomial Functions



$$-x=0 \quad x+1=0 \quad x-2=0$$

Examples

$$1. \quad f(x) = -x(x+1)^2(x-2)^2$$

<u>z</u>	<u>m</u>	<u>tors</u>	<u>d</u>
0	1 odd	C	$1+2+2$
-1	2 even	T	<u>5</u>
2	2 even	T	<u>=</u>

max zeros: 5      end behavior  
 max intercepts: 5  
 turning pts: 4

pt in region:  $-1 \rightarrow 0$ 

$$(-\frac{1}{2}) \rightarrow f(-\frac{1}{2}) \rightarrow (-\frac{1}{2})(-\frac{1}{2}+1)^2(-\frac{1}{2}-2)^2$$

$$\cdot (-\frac{1}{2})(\frac{1}{2})^2(\frac{-5}{2})^2$$

$$(\frac{1}{2})(\frac{1}{4})(\frac{25}{4}) = \frac{25}{32}$$

pt in region  $0 \rightarrow 2$ 

$$f(1) = (-1)(1+1)^2(1-2)^2$$

$$f(1) = (-1)(4)(1) = -4$$

$$(1, -4)$$

$$2. \quad f(x) = -x\underline{(x-2)(x-2)}(x+3)$$

$\underline{\text{m}}$   $\underline{\text{t or C}}$   $\underline{\text{D}}$

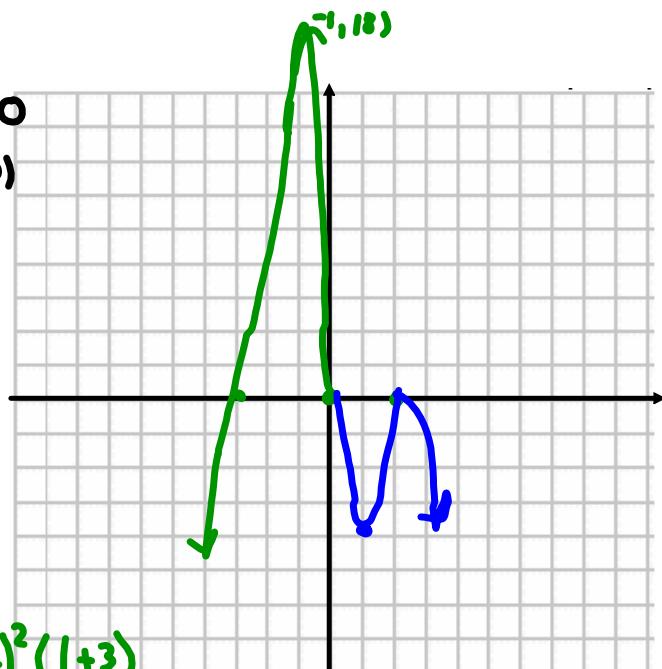
$x$	$m$	$t \text{ or C}$	$D$	$y_{\text{int}}(0,0)$
0	$1 \rightarrow 0$	C	$1+2+1$	
2	$2 \rightarrow E$	t	$\underline{4+4}$	
-3	$1 \rightarrow 0$	C		

max zeros: 4  
 max intercepts 4  
 max t.pts 3

end behavior even  $\rightarrow$  Neg

$f(-1) = -(-1)(-1-2)^2(1+3)$   
 $f(-1) = (1)(9)(2)$   
 $f(-1) = 18$

$f(1) = -(1)(1-2)^2(1+3)$   
 $f(1) = -4$



3.  $f(x) = \cancel{x^3 + 2x^2 - x - 2}$

$f(x) = x^2(x+2) - 1(x+2)$

$f(x) = (x+2)(x^2 - 1)$

$f(x) = (x+2)(x+1)(x-1)$

$\infty$	$m$	$t$ or $c$	$D$	<u>end behavior</u>
-2	1	$\downarrow$	$\uparrow$	$0 \rightarrow 1 \rightarrow +$
-1	1	$\downarrow$	$\uparrow$	
1	1	$\uparrow$	$\downarrow$	

points in region

-2 and -1

$f(-3) =$

$(-\frac{1}{2})(-\frac{1}{2})(-\frac{1}{2}) = \frac{1}{8}$

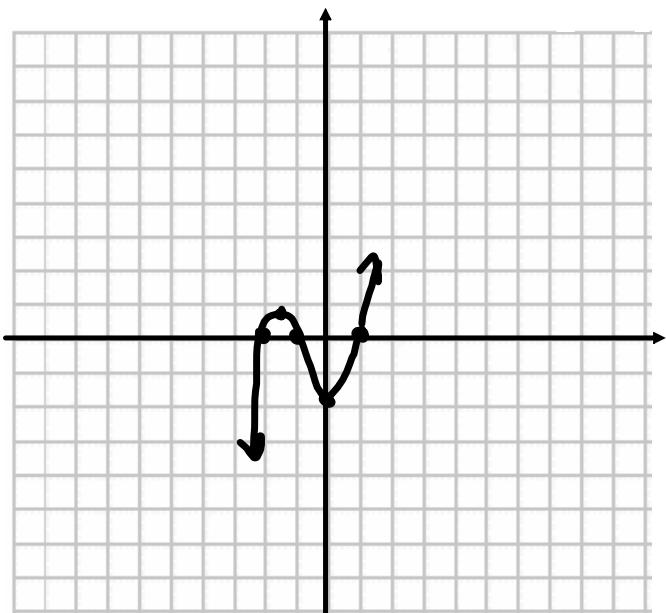
$(-3, \frac{1}{8})$

.1 and 1

$f(0) = -2$

$(-1.5+2)(1.5+1)(-1.5-1)$

$y_{int}: (0, -2)$



HW: P. 283 # 2, 4, 6, 7 - 12  
(do without calculator)  
# 13, 20, 21  
P. 270 # 11, 13, 34

Graded due Tomorrow