

Homework 7-5

1. 4

2a. $7/25$ b. $-24/25$ c. $-7/24$ d. 163.7°

3a. $-5/13$ b. $-12/13$ c. $5/12$ d. 202.6°

4. $\sin(\theta) = -3/5$ $\cos(\theta) = -4/5$ $\tan(\theta) = 3/4$

5. $\sin(\theta) = 5/\sqrt{29}$ $\cos(\theta) = -2/\sqrt{29}$ $\tan(\theta) = -5/2$

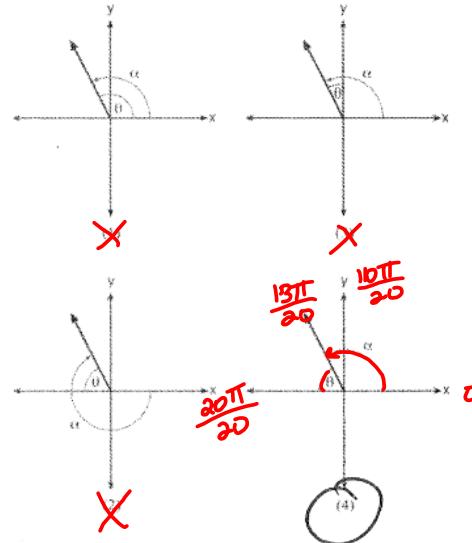
6. A 7. 3

Name: Kelly
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Algebra 2 Homework 7-5

1. Which diagram (right) represents an angle, α , measuring $\frac{13\pi}{20}$ radians drawn in standard position, and its reference angle, θ ? (Regents question)

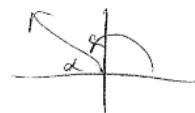
Here, α = whole *
 θ = Ref *
 (opposite of normal notation)



- For #2 - 4:
- What is $\sin(\theta)$?
 - What is $\cos(\theta)$?
 - What is $\tan(\theta)$?
 - Find angle θ to the nearest tenth.

2. The angle θ corresponds to the angle between the positive x-axis and the line between the origin and the point $\left(\frac{-24}{25}, \frac{7}{25}\right)$ on the unit circle. State your answers as exact expressions. Q.II

a) $\frac{7}{25}$ c) $\frac{7/25}{-24/25} = -\frac{7}{24}$
 b) $-\frac{24}{25}$ d) $\theta = \sin^{-1}\left(\frac{7}{25}\right) = 16.3^\circ$
 $\theta = 180 - 16.3 = 163.7^\circ$

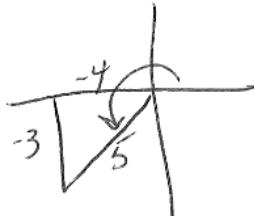


3. The angle θ corresponds to the angle between the positive x-axis and the line between the origin and the point $\left(\frac{-12}{13}, \frac{-5}{13}\right)$ on the unit circle. State your answers as exact expressions.

a) $-\frac{5}{13}$ c) $\frac{-5/13}{-12/13} = \frac{5}{12}$
 b) $-\frac{12}{13}$ d) $\theta = \sin^{-1}\left(\frac{5}{13}\right) = 22.6^\circ$
 $\theta = 180 + 22.6 = 202.6^\circ$



4. P(-4, -3) is a point on the terminal side of θ in standard position. Find the exact values of $\sin(\theta)$, $\cos(\theta)$ and $\tan(\theta)$.

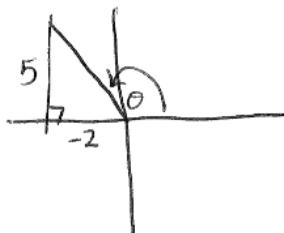


$$\sin(\theta) = \frac{-3}{5}$$

$$\cos(\theta) = \frac{-4}{5}$$

$$\tan(\theta) = \frac{-3}{-4} = \frac{3}{4}$$

5. P(-2, 5) is a point on the terminal side of θ in standard position. Find the exact values of $\sin(\theta)$, $\cos(\theta)$ and $\tan(\theta)$.



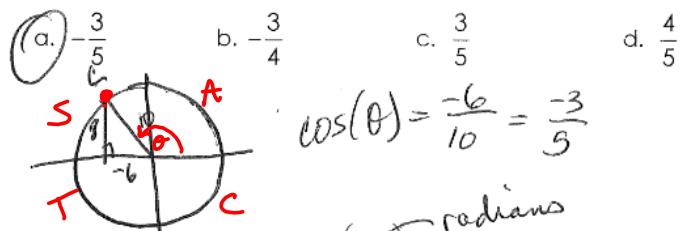
$$\begin{aligned} 2^2 + 5^2 &= x^2 \\ 4 + 25 &= x^2 \\ \sqrt{29} &= x \end{aligned}$$

$$\sin(\theta) = \frac{5}{\sqrt{29}}$$

$$\cos(\theta) = \frac{-2}{\sqrt{29}}$$

$$\tan(\theta) = \frac{5}{-2}$$

6. A circle centered at the origin has a radius of 10 units. The terminal side of an angle, θ , intercepts the circle in Quadrant II at point C. The y-coordinate of point C is 8. What is the value of $\cos(\theta)$? (Regents question)



$$\cos(\theta) = \frac{-6}{10} = -\frac{3}{5}$$

7. The function $f(x) = 2^{-0.25x} \cdot \sin\left(\frac{\pi}{2}x\right)$ represents a damped sound wave function. What is the

average rate of change for this function on the interval $[-7, 7]$, to the nearest hundredth?

(Regents Question)

- (1) -3.66
(2) -0.30

- (3) -0.26
(4) 3.36

$$f(7) = 2^{-0.25(7)} \sin\left(\frac{\pi}{2}(7)\right) = -2.297$$

$$f(-7) = 2^{-0.25(-7)} \sin\left(\frac{\pi}{2}(-7)\right) = 3.364$$

$$\text{Ref C} = \frac{\Delta y}{\Delta x} = \frac{-2.297 - 3.364}{7 - (-7)} = -26.5$$

Day 6: Pythagorean Identity

Pythagorean Theorem: $a^2 + b^2 = c^2$

On the unit circle: $x^2 + y^2 = 1$

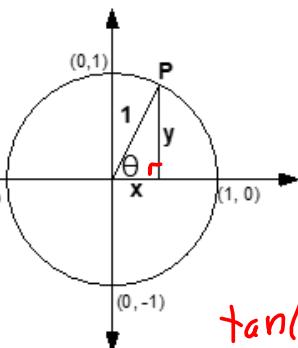
Remember: $x = \cos(\theta)$ and $y = \sin(\theta)$, so...

Pythagorean Identity: $(\cos(\theta))^2 + (\sin(\theta))^2 = 1$

$$\sin^2(\theta) + \cos^2(\theta) = 1$$

$$\sin^2(\theta) = (\sin(\theta))^2$$

in calculator



$$\tan(\theta) = \frac{\sin(\theta)}{\cos(\theta)}$$

Examples:

1. Using the Pythagorean Identity, given $\sin(\theta) = .6$, find $|\cos(\theta)|$ and $|\tan(\theta)|$.

$$\begin{aligned}\sin^2(\theta) + \cos^2(\theta) &= 1 \\ (.6)^2 + \cos^2(\theta) &= 1 \\ .36 + \cos^2(\theta) &= 1 \\ \sqrt{\cos^2(\theta)} &= \sqrt{.64} \\ \cos(\theta) &= \pm .8\end{aligned}$$

$$\tan(\theta) = \frac{\sin(\theta)}{\cos(\theta)}$$

$$|\cos(\theta)| = .8$$

$$|\tan(\theta)| = \frac{|\sin(\theta)|}{|\cos(\theta)|} = \frac{.6}{.8} = \frac{3}{4} \text{ or } .75$$

2. Using the Pythagorean Identity, given $\cos(\theta) = 5/13$, and angle θ is in quadrant IV, find $\sin(\theta)$ and $\tan(\theta)$.

$$\begin{aligned}\sin^2(\theta) + \cos^2(\theta) &= 1 \\ \sin^2(\theta) + \left(\frac{5}{13}\right)^2 &= 1 \\ \sin^2(\theta) + \frac{25}{169} &= \frac{169}{169} \\ \sqrt{\sin^2(\theta)} &= \sqrt{\frac{144}{169}} \\ \sin(\theta) &= \pm \frac{12}{13}\end{aligned}$$



in Quad III:

$$(\rightarrow \sin(\theta) = -\frac{12}{13})$$

$$(\rightarrow \tan(\theta) = \frac{-12/13}{5/13} = -\frac{12}{5})$$

3. Using the identity $\sin^2(\theta) + \cos^2(\theta) = 1$, if $\cos(\theta)$ is -0.7 and θ is in Quad. II,

a. Find $\sin(\theta)$ to the nearest tenth.

$$\sin^2(\theta) + (-.7)^2 = 1$$

$$\sin^2(\theta) + .49 = 1$$

$$\sqrt{\sin^2(\theta)} = \sqrt{.51}$$

$$\sin(\theta) = \pm .7$$

$$\text{QII: } \sin(\theta) = +.7$$

b. Find $\tan(\theta)$ and $m < \theta$ to the nearest tenth.

$$\tan(\theta) = \frac{\sin(\theta)}{\cos(\theta)} = \frac{.7}{-.7} = -1$$

$$\alpha = \tan^{-1}(1) = 45^\circ$$

$$\theta = 180^\circ - 45^\circ = 135^\circ$$



4. If $\sin^2(32^\circ) + \cos^2(M) = 1$, then M equals
 a. 32° b. 58° c. 68° d. 72°

5. Using the Pythagorean Identity, given $\cos(\theta) = -0.5$, and angle θ is in quadrant III, find $\sin(\theta)$ and $\tan(\theta)$ to the nearest tenth.

$$\sin^2(\theta) + \cos^2(\theta) = 1$$

$$\sin^2(\theta) + (-.5)^2 = 1$$

$$\sin^2(\theta) + .25 = 1$$

$$\sqrt{\sin^2(\theta)} = \sqrt{.75}$$

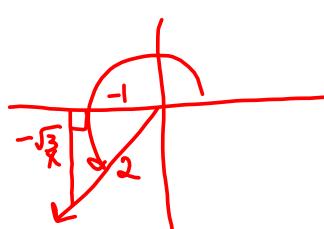
$$\tan(\theta) = \frac{-0.9}{-.5} = 1.8$$



$$\sin(\theta) = \pm .866 = \pm .9$$

$$\text{QIII } \sin(\theta) = -.9$$

6. Draw an angle in standard position given $\cos(\theta) = -1/2$, and angle θ is in quadrant III. Use the triangle to find $\sin(\theta)$ and $\tan(\theta)$ to the nearest tenth.



$$\begin{aligned} 1^2 + x^2 &= 2^2 \\ 1 + x^2 &= 4 \\ \sqrt{x^2} &= \sqrt{3} \\ x &= \sqrt{3} \end{aligned}$$

$$\begin{aligned} \sin(\theta) &= -\sqrt{3}/2 \\ \tan(\theta) &= -\sqrt{3}/-1 = \sqrt{3} \end{aligned}$$

7. Using the Pythagorean Identity, given $\sin(\theta) = -7/10$, and angle θ is in quadrant IV, find the exact values of $\cos(\theta)$ and $\tan(\theta)$.

$$\begin{aligned} \sin^2(\theta) + \cos^2(\theta) &= 1 \\ \left(-\frac{7}{10}\right)^2 + \cos^2(\theta) &= 1 \\ \frac{49}{100} + \cos^2(\theta) &= 1 - \frac{100}{100} \\ \sqrt{\cos^2(\theta)} &= \sqrt{\frac{51}{100}} \quad \cancel{\pm \sqrt{100}} \\ \cos(\theta) &= \pm \frac{\sqrt{51}}{10} \end{aligned}$$

$$\begin{aligned} \text{Q IV (+)} \rightarrow \cos(\theta) &= \frac{\sqrt{51}}{10} \\ \tan(\theta) &= \frac{-7/10}{\sqrt{51}/10} = \frac{-7}{\sqrt{51}} \end{aligned}$$

8. If $\sin^2(\theta) + \cos^2(\theta) = 1$, then θ equals

- a. $-\theta$ b. $\pi/3$ c. π d. $\pi/2$