



Applications of the Rules of Exponents with Word Problems

Applications of the Rules of Exponents with Word Problems Unit 9 Day 11

Percents and phenomena that grow at a constant percent rate can be challenging, to say the least. This is due to the fact that, unlike linear phenomena, the growth rate indicates a constant multiplier effect instead of a constant additive effect (linear). Because constant percent growth is so common in everyday life (not to mention in science, business, and other fields), it's good to be able to **mindfully manipulate percent**.

Exercise #1: A population of kangaroos is growing at a constant percent rate. If the population on January 1st is 1027 and a year later is 1079, what is its yearly percent growth rate to the nearest tenth of a percent?

$$\begin{aligned}A(t) &= a(1 \pm r)^t \\ \frac{1079}{1027} &= \frac{1027(1+r)}{1027} \\ 1.0506 &= 1+r \\ .0506 &= r \\ \times 100 \\ 5.06 &\sim \textcircled{5.1\%}\end{aligned}$$

Exercise #2: Now let's try to determine what the percent growth in the kangaroo population will be over a decade^{10 yrs} of time. We will assume that the rounded percent increase found in Exercise #1 continues for the next decade.

(a) After 10 years, what will we have multiplied the original population by, rounded to the nearest hundredth?

$$\begin{aligned} &(1 + .051)^t \\ &(1.051)^t \\ &(1.051)^{10} \\ &1.64 \end{aligned}$$

(b) Using your answer from (a), what is the decade percent growth rate?

64%

Exercise #3: Let's stick with our kangaroos from Exercise #1. Assuming their growth rate is constant over time, what is their monthly growth rate to the nearest tenth of a percent? Assume a constant sized month.

$$\begin{aligned} & (1.051)^y \\ & \left((1.051)^{\frac{1}{12}m} \right)^{12} \\ & 1.004^m \\ & \textcircled{.4\%} \end{aligned}$$

$$\begin{aligned} m &= 12y \\ \left(\frac{1}{12}m \right) &= y \end{aligned}$$

$$(2^2)^3 = 2^{2 \cdot 3}$$

Exercise #4: If a population was growing at a constant rate of 22% every 5 years, then what is its percent growth rate over a 2-year time span? Round to the nearest tenth of a percent.

(a) First, give an expression that will calculate the single year (or yearly) percent growth rate based on the fact that the population grew 22% in 5

(b) Now use this expression to calculate the percent growth over 2 years.

Exercise #5: Last year the total revenue for Wegmans increased by 6.25% over the previous year. If this trend were to continue, which expression could the company's chief financial officer use to approximate their monthly percent increase in revenue? (Let m represent months.)

1. $(1.0625)^m$
2. $(1.0625)^{12/m}$
3. $(1.00506)^m$
4. $(1.00506)^{m/12}$

$$1.0625^{1/2}$$

Exercise #6: A study of the annual population of the red-winged blackbird in Ft. Mill, South Carolina, shows the population, $B(t)$, can be represented by the function $B(t) = 750(1.16)^t$, where the t represents the number of years since the study began.

In terms of the monthly rate of growth, the population of red-winged blackbirds can be best approximated by the function

1. $B(t) = 750(1.012)^t$
2. $B(t) = 750(1.012)^{12t}$
3. $B(t) = 750(1.16)^{12t}$
4. $B(t) = 750(1.16)^{t/12}$

$$1.16^{1/12} = 1.012$$

Exercise #7: Iridium-192 is an isotope of iridium and has a half-life of 73.83 days. If a laboratory experiment begins with 100 grams of Iridium-192, the number of grams, A , of Iridium-192 present after t days would be $A = 100 \left(\frac{1}{2} \right)^{\frac{t}{73.83}}$. Which equation approximates the amount of Iridium-192 present after t days?

1. $A = 100 \left(\frac{73.83}{2} \right)^t$

2. $A = 100 \left(\frac{1}{147.66} \right)^t$

3. $A = 100(0.990656)^t$

4. $A = 100(0.116381)^t$

$$\left(\left(\frac{1}{2} \right)^{\frac{1}{73.83}} \right)^t = .990656$$

or sub in
 $X = \underline{\hspace{2cm}}$

Exercise #8: An equation to represent the value of a car after t months of ownership is $v = 32,000(0.81)^{\frac{t}{12}}$. Which statement is not correct?

1. The car lost approximately 19% of its value each ~~month~~ ^{year}.
2. The car maintained approximately 98% of its value each month.
3. The value of the car when it was purchased was \$32,000.
4. The value of the car 1 year after it was purchased was \$25,920.

$$32000(.81)^{12/12}$$

$$\left(\begin{array}{c} (.81)^{1/12} \\ (.98) \end{array} \right)^m$$

HW 9-10

1. (2) \$192
2. Setauket Equation $S(t) = 6200(1.08)^t$ During the 18th year or by the 19th
Stony Brook Equation $B(t) = 8750(1.06)^t$ year.
See windows, graph, and tables on the next slides
3. \$247
4. Option A $A(n) = 10000(1.035)^n$
Option B $B(n) = 10000(1 + .0325/4)^{4n}$
Option A by \$932.22
5. 4%

Name _____

Alg 2 HW 9-10

1. If \$130 is invested in a savings account that earns 4% interest per year, which of the following is closest to the amount in the account at the end of 10 years?

(1) \$218

(3) \$168

(2) \$192

(4) \$324

$$\begin{aligned} A(t) &= 130(1.04)^t \\ A(10) &= 130(1.04)^{10} \\ &= \$192.43 \end{aligned}$$

2. Setauket has a population of 6,200 people and is growing at a rate of 8% per year. Stony Brook has a population of 8,750 and is growing at a rate of 6% per year. In how many years, to the nearest year, will Setauket have a greater population than Stony Brook? Show the equation or inequality you are solving and solve it graphically.

Setauket Equation $S(t) = 6200(1.08)^t$

Stony Brook Equation $B(t) = 8750(1.06)^t$

Setauket Window

x-min 0

x-max 30

y-min 0

y-max 40000

Stony Brook Window

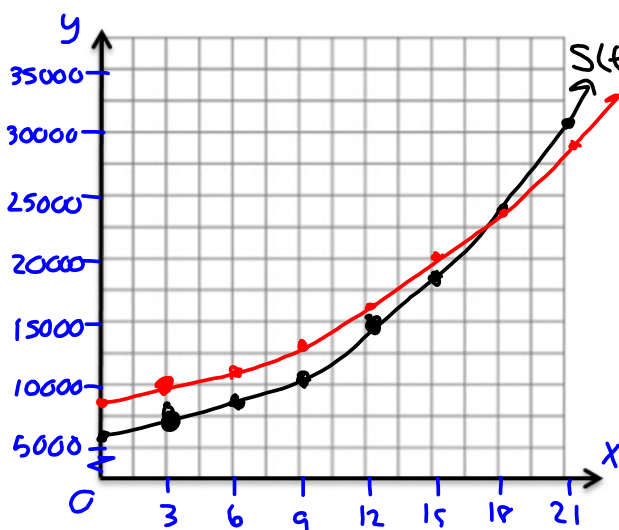
x-min 0

x-max 30

y-min 0

y-max 40000

Values
may
vary



Setauket

$S(t)$

$B(t)$

x

y

Stony Brook

x

y

0

3

6

9

12

15

18

21

0

3

6

9

12

15

18

21

0

3

6

9

12

15

18

21

3. \$200 is deposited in a bank account. The interest is compounded monthly at a rate of 4.25%. How much money is in the account after 5 years, to the nearest dollar?

$$\begin{aligned} a &= \$200 \\ r &= .0425 \\ t &= 5 \end{aligned} \quad A(5) = 200 \left(1 + \frac{.0425}{12} \right)^{12(5)} = \$247$$

4. Ben's parents gave him \$10,000 for his 18th birthday. He is considering two investment options.

Option A will pay him 3.50% interest compounded annually. Option B will pay him 3.25% interest

compounded quarterly. Write a function of Option A and Option B that calculates the value after n years.

Option A $A(n) = 10000(1.035)^n$

Option B $B(n) = 10000 \left(1 + \frac{.0325}{4} \right)^{4n}$

Ben wants to use the money in 22 years to buy a sports car. Determine which plan would yield the greatest return and by how much.

$$\begin{aligned} A(22) &= 10000(1.035)^{22} \\ &= \$21315.11 \end{aligned}$$

Option A by
\$932.22

$$B(22) = 10000 \left(1 + \frac{.0325}{4} \right)^{4(22)} = \$20382.89$$

5. A house purchased 10 years ago for \$80,000 was just sold for \$120,000. Assuming exponential growth, approximate the annual growth rate, to the nearest percent.

$$\frac{120,000}{80,000} = \frac{80,000(1+r)^{10}}{80,000}$$

$$\sqrt[10]{1.5} = \sqrt[10]{(1+r)^{10}}$$

$$\begin{array}{r} 1.04 = 1+r \\ \hline -1 \quad \quad -1 \end{array}$$

$$r = .04$$

$$\textcircled{4\%}$$