

## Unit 10 Day 3 HW

1. See graph on next slide.

~~(1, 2)~~

~~(2, 1)~~

~~(3, 2)~~

6. (2)

7. (1)

8. (4)

9.  $x = \frac{1}{2}$

10.  $x = 7$

2.  $3\log x + \log y$

3.  $\frac{1}{2} \log a - \log b$

4.  $3 \log x + \log y - 2 \log z$

5.  $2 \log r - \log s - \frac{1}{2} \log t$

Name \_\_\_\_\_

Alg 2 CC

Date \_\_\_\_\_

Unit 10 Day 3 HW

1. Graph  $y = \log_3(x+1)+2$  left 1, up 2

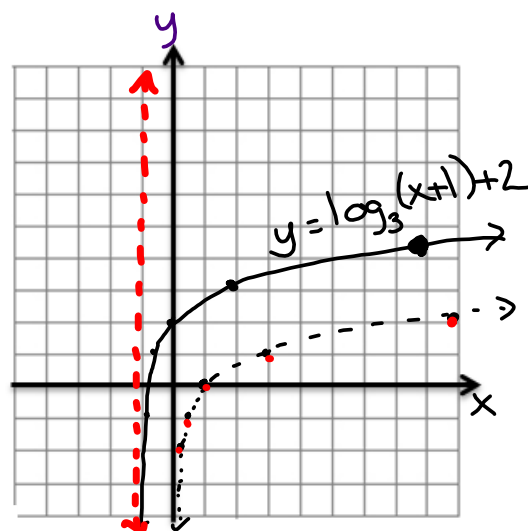
Hint use the inverse to find your coordinates to plot.

$$y = 3^x$$

|   |               |               |   |   |   |
|---|---------------|---------------|---|---|---|
| x | -2            | -1            | 0 | 1 | 2 |
| y | $\frac{1}{9}$ | $\frac{1}{3}$ | 1 | 3 | 9 |

|   |               |               |   |   |   |
|---|---------------|---------------|---|---|---|
| x | $\frac{1}{9}$ | $\frac{1}{3}$ | 1 | 3 | 9 |
| y | -2            | -1            | 0 | 1 | 2 |

$$y = \log_3 x$$



Use the laws of logarithms to expand questions 2 - 5.

$$2. \log x^3 y = 3 \log x + \log y$$

$$3. \log \frac{\sqrt{a}}{b} = \log a^{1/2} - \log b = \frac{1}{2} \log a - \log b$$

$$4. \log \frac{x^3 y}{z^2} = \log x^3 + \log y - \log z^2 = 3 \log x + \log y - 2 \log z$$

$$5. \log \frac{r^2}{s \sqrt{t}} = \log r^2 - (\log s + \log t^{1/2}) \\ = 2 \log r - \log s - \frac{1}{2} \log t$$

6. Which of the following is equivalent to  $\log_3(9x)$ ?

(1)  $\log_3 2 + \log_3 x$

(2)  $2 + \log_3 x$

(3)  $2\log_3 x$

(4)  $x + \log_3 2$

$$\log_3 9 + \log_3 x$$

$$2 + \log_3 x$$

~~$$\log_3 9 = x$$~~

$$3^x = 9 \quad 3^x = 3^2$$

$$x = 2$$

7. The expression of  $\log \frac{x^2}{10}$  is equivalent to

(1)  $2 \log x - 1$

(2)  $2 \log x - 10$

(3)  $\log 2x - 1$

(4)  $\log 2x - 10$

$$\log x^2 - \log 10$$

$$2 \log x - \log 10$$

$$2 \log x - 1$$

8. If  $f(x) = \log x$  and  $g(x) = 100x^3$ , then  $f(g(x)) =$

(1)  $100 \log x$

(2)  $300 \log x$

(3)  $6 + \log x$

(4)  $2 + 3 \log x$

$$= \log(100x^3)$$

$$= \log 100 + \log x^3$$

$$= \log 100 + 3 \log x$$

$$= 2 + 3 \log x$$

9. Solve for x.

$$5^{4x-5} = \frac{1}{125}$$

$$5^{4x-5} = 5^{-3}$$

$$4x - 5 = -3$$

$$\begin{array}{r} +5 \\ \hline \end{array}$$

$$\frac{4x}{4} = \frac{2}{4} \quad x = \frac{1}{2}$$

$$\left\{ \frac{1}{2} \right\}$$

10. Algebraically determine the zeroes of the exponential function

$f(x) = 2^{2x-9} - 32$ . Recall that the reason it is known as a zero is because the output is zero.

$$\begin{array}{r} 0 = 2^{2x-9} - 32 \\ +32 \quad \quad +32 \\ \hline 32 = 2^{2x-9} \end{array}$$

$$\begin{array}{r} 2^5 = 2^{2x-9} \\ 5 = 2x - 9 \quad x = 7 \\ \begin{array}{r} +9 \quad \quad +9 \\ \hline 14 = 2x \\ \frac{14}{2} = \frac{2x}{2} \end{array} \quad \{7\} \end{array}$$

## More Properties of Logarithms

## More Properties of Logs

## Unit 10 Day 4

## Warm-up

The expression of  $\log\left(\frac{x^2}{1000}\right)$  can be written in equivalent form as

(1)  $2\log x - 3$

(2)  $2\log x - 6$

(3)  $\log 2x - 3$

(4)  $\log 2x - 6$

$$\begin{aligned} & \log x^2 - \log 1000 \\ & 2\log x - 3 \end{aligned}$$

## More Properties of Logs

Unit 10 Day 4

Reverse Rules of Logs "Squish"

$$\log a + \log b = \log(ab)$$

$$\log a - \log b = \log\left(\frac{a}{b}\right)$$

$$n \log a = \log a^n$$

$$\frac{1}{n} \log a = \log a^{\frac{1}{n}} = \log \sqrt[n]{a}$$



Express as a single logarithm:

1.  $2 \log a - \log b = \log a^2 - \log b = \log \left( \frac{a^2}{b} \right)$

2.  $\log a - \frac{1}{2} \log b = \log a - \log \sqrt{b} = \log \left( \frac{a}{\sqrt{b}} \right)$

3.  $3 \log x + \frac{1}{2} \log y = \log x^3 + \log \sqrt{y}$   
 $\log(x^3 \sqrt{y})$

$$4. \log x^3 y^5 - \log xy^3 = \log \left( \frac{x^3 y^5}{xy^3} \right) = \log (x^2 y^2)$$

$$5. \log a - \frac{1}{3}\log b - \frac{1}{3}\log c = \log a - \log \sqrt[3]{b} - \log \sqrt[3]{c} \\ = \log \left( \frac{a}{\sqrt[3]{bc}} \right)$$

Change of Base Law:

$$\log_B A = \frac{\log A}{\log B}$$

"Base 10"  
use calculator

Evaluate. Give an exact value where possible, otherwise round to four decimal places.

$$5. \log_9 27 = \frac{\log 27}{\log 9} = 1.5$$

$$6. \log_{32} 8 = \frac{\log 8}{\log 32} = .6$$

$$7. \log_4 87 = \frac{\log 87}{\log 4} = 3.2215$$

Express as a single logarithm. Simplify if possible.

$$8. \log_6 3 + \log_6 2 = \log_6 (3 \cdot 2) = \log_6 6 = \frac{\log 6}{\log 6} = 1$$

$$9. \log_8 16 + \log_8 4 = \log_8 (16 \cdot 4) = \log_8 64 = \frac{\log 64}{\log 8} = 2$$

$$11. \log_8 80 + \log_8 51.2 = \log_8 (80 \cdot 51.2) = \log_8 4096 = \frac{\log 4096}{\log 8} = 4$$

$$12. \log 2 + \log 25 - \log 5 = \log (2 \cdot 25 / 5) = \log_{10} 10 = 1$$

13. Which of the following is not equivalent to  $\log 36$ ?

(1)  $\log 2 + \log 18$

(3)  $2\log 6$

(2)  $\log 30 + \log 6$

(4)  $\log 4 + \log 9$

14. If  $\log 5 = p$  and  $\log 2 = q$  then  $\log 200$  can be written in terms of  $p$  and  $q$  as

(1)  $4p + q$

(3)  $2p + 3q$

(2)  $2(p + q)$

(4)  $3p + 2q$

$\log 200 = \log(25 \cdot 8)$   
 $\log 200 = \log(5^2 \cdot 2^3) = 2\log 5 + 3\log 2$

Calc:  $2(\log 5) + 3(\log 2) = \log 200$

