

Day 1: Right Triangles

$$\sin(A) = \frac{\text{oppo}}{\text{hyp}}$$

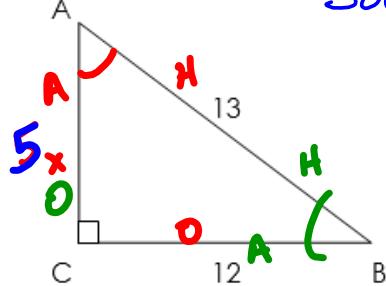
$$\cos(A) = \frac{\text{adj}}{\text{hyp}}$$

$$\tan(A) = \frac{\text{oppo}}{\text{adj}}$$

$$a^2 + b^2 = c^2$$

What mnemonic do you use?

Soh Cah Toa S $\frac{O}{H}$ C $\frac{A}{H}$ T $\frac{O}{A}$



$$\begin{array}{ll} \sin(A) = \frac{12}{13} & \sin(B) = \frac{5}{13} \\ \cos(A) = \frac{5}{13} & \cos(B) = \frac{12}{13} \\ \tan(A) = \frac{12}{5} & \tan(B) = \frac{5}{12} \end{array}$$

$$\begin{aligned} x^2 + 12^2 &= 13^2 \\ x^2 + 144 &= 169 \\ x^2 &= 25 \\ x &= 5 \end{aligned}$$

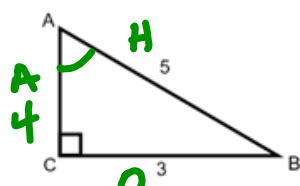
1. Find $\sin(A)$, $\cos(A)$, $\tan(A)$ and $m\angle A$ to nearest degree.

$$\sin(A) = \frac{3}{5}$$

$$\cos(A) = \frac{4}{5}$$

$$\tan(A) = \frac{3}{4}$$

$$m\angle A = \sin^{-1}\left(\frac{3}{5}\right) = 37^\circ$$



$$\begin{aligned} 3^2 + x^2 &= 5^2 \\ 9 + x^2 &= 25 \\ x^2 &= 16 \\ x &= 4 \end{aligned}$$

$\{3, 4, 5\}$
 $\{5, 12, 13\}$
 $\{8, 15, 17\}$

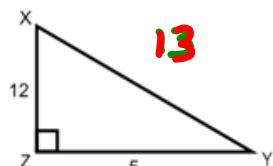
2. Find $\cos(X)$, $\sin(X)$, $\tan(Y)$ and $m\angle X$ to nearest degree.

$$\cos(X) = \frac{12}{13}$$

$$\sin(X) = \frac{5}{13}$$

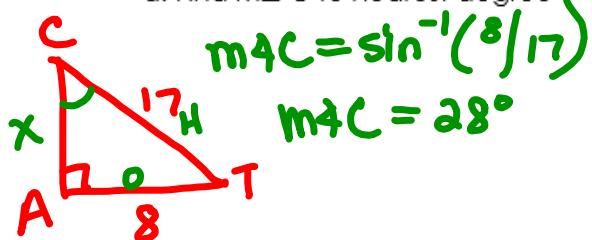
$$\tan(Y) = \frac{12}{5}$$

$$m\angle X = \cos^{-1}\left(\frac{12}{13}\right) = 23^\circ \quad \text{or } \sin^{-1}\left(\frac{5}{13}\right)$$



3. Given $\triangle CAT$ with hypotenuse CT. The side opposite $\angle C$ is 8 units long and the hypotenuse is 17 units long.

a. Find $m\angle C$ to nearest degree



$$\sin C = \frac{8}{17}$$

$$m\angle C = 28^\circ$$

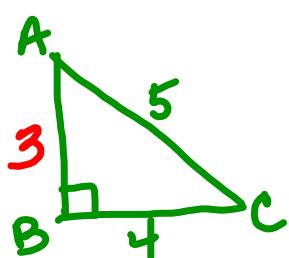
b. Use $m\angle C$ to find side CA

$$\cos(28^\circ) = \frac{x}{17}$$

$$x = 17 \cos(28^\circ)$$

$$x = 15$$

4. Sketch triangle ABC, where angle B is the right angle and $\sin(A) = \frac{4}{5}$. Then find $\cos(A)$ and $\tan(A)$.

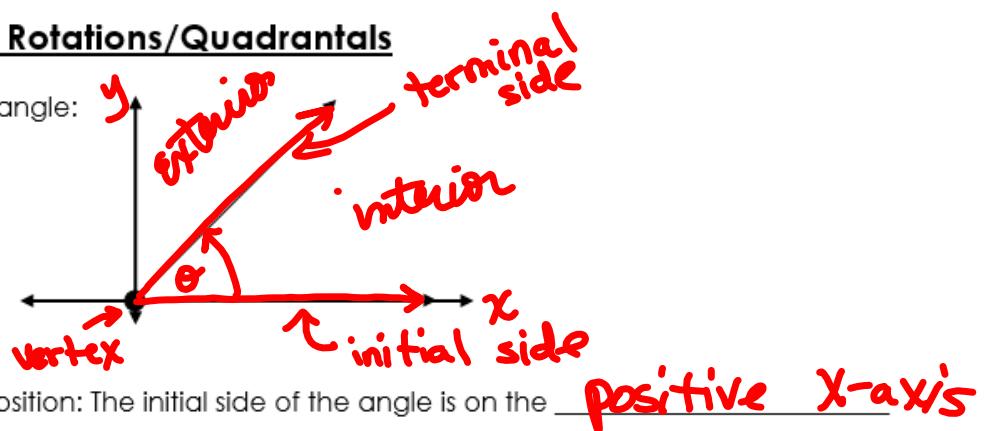


$$\sin(A) = \frac{3}{5}$$

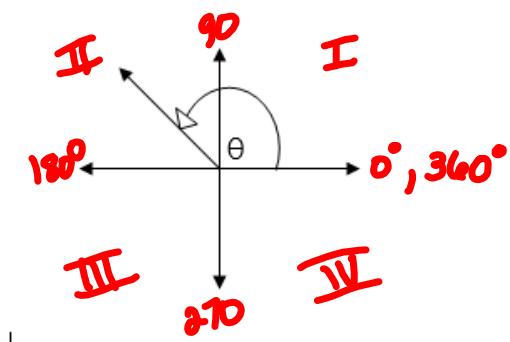
$$\tan(A) = \frac{4}{3}$$

Angle of Rotations/Quadrantal

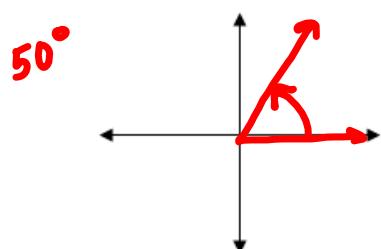
Parts of an angle:

Standard Position: The initial side of the angle is on the positive x-axis

θ = Greek letter "theta" (a variable commonly used for angles)

Measures of $\angle \theta$ in:

Quad I	$0^\circ < \theta < 90^\circ$
Quad II	$90^\circ < \theta < 180^\circ$
Quad III	$180^\circ < \theta < 270^\circ$
Quad IV	$270^\circ < \theta < 360^\circ$

Degree MeasurePositive angle: counter-clockwise directionNegative angle: clockwise direction