

Warm-up Not In Notes

$$16x + 2x = 18$$

$$16+2x$$

Is $16 + 2\sqrt{10} = 18\sqrt{10}$? Not true because the left side cannot be combined...no like terms
 Prove to your neighbor why or why not.

$$(16+2)\sqrt{10} = 18\sqrt{10}$$

$$16\sqrt{10} + 2\sqrt{10} = 18\sqrt{10}$$

Aug 15-10:55 AM

3. $5\sqrt{3}$

1 & 2. Look at next page

1-10 HW Answer Key

4. -22

5. $2\sqrt{7}$

6. $\sqrt{14}$

7. $\sqrt{3}$

8. $3\sqrt{2}$

9. 64, 8

10. 16, 4

11. 48, $4\sqrt{3}$

12. 117, $3\sqrt{13}$

13. $3x(2x-5)(x+2)$

14. {0, 5, -2}

15. $(2x+5)(4x^2-10x+25)$

Aug 28-12:25 PM

1. Justify that $\sqrt{a} \cdot \sqrt{b} = \sqrt{ab}$ by letting a=25 and b=4.

$$\begin{aligned}\sqrt{25+14} &\stackrel{?}{=} \sqrt{25 \cdot 4} \\ 5+2 &= \sqrt{100} \\ 10 &= 10 \checkmark\end{aligned}$$

2. Justify that $\sqrt{\frac{a}{b}} = \frac{\sqrt{a}}{\sqrt{b}}$ by letting a=100 and b=4.

$$\begin{aligned}\sqrt{\frac{100}{4}} &\stackrel{?}{=} \frac{\sqrt{100}}{\sqrt{4}} \\ \sqrt{25} &= \frac{10}{2} \\ 5 &= 5 \checkmark\end{aligned}$$

Express in simplest radical form.

3. $\sqrt{75} = \sqrt{25} \sqrt{3}$
 $= 5\sqrt{3}$

4. $-2\sqrt{121} = -2(11) = -22$

5. $\frac{\sqrt{56}}{\sqrt{2}} = \sqrt{28}$
 $= \sqrt{4 \cdot 7}$
 $= 2\sqrt{7}$

$$\sqrt{\frac{56}{2}} = \sqrt{28}$$

6. $\frac{\sqrt{56}}{2} = \frac{\sqrt{4 \cdot 14}}{2} = \frac{2\sqrt{14}}{2} = \sqrt{14}$

7. $\sqrt{\frac{36}{12}} = \sqrt{3}$

8. $\frac{3}{4}\sqrt{32} = \frac{3}{4}\sqrt{16} \sqrt{2} = 3\sqrt{2}$

Sep 1-4:32 PM

b^2-4ac
Find the discriminant and then take its square root.

9. $5x^2 + 2x - 3 = 0$
 $b^2 - 4ac = (-2)^2 - 4(5)(-3)$
 $= 4 + 60$
 $= 64$
 $\sqrt{64} = 8$

10. $3x^2 - 10x + 7 = 0$
 $b^2 - 4ac = (-10)^2 - 4(3)(7)$
 $= 100 - 84$
 $\sqrt{16} = 4$

11. $2x^2 - 4x = 4$
 $2x^2 - 4x - 4 = 0$
 $b^2 - 4ac = (-4)^2 - 4(2)(-4)$
 $= 16 + 32$
 $= 48$
 $\sqrt{48} = \sqrt{16 \cdot 3} = 4\sqrt{3}$

12. $9x^2 + 3x = 3$
 $9x^2 + 3x - 3 = 0$
 $b^2 - 4ac = 3^2 - 4(9)(-3)$
 $= 9 + 108$
 $= 117$
 $\sqrt{117} = \sqrt{9 \cdot 13} = 3\sqrt{13}$

$a=9$
 $b=3$
 $c=-3$
 $x_1 = \frac{-b + \sqrt{b^2 - 4ac}}{2a}$
 $y_1 = \frac{-b - \sqrt{b^2 - 4ac}}{2a}$

13. Factor completely: $6x^3 - 3x^2 - 30x = 3x(2x^2 - x - 10)$
 $= 3x[2x^2 - 5x + 4(x-10)]$
 $= 3x[x(2x-5) + 2(2x-5)]$
 $= 3x(2x-5)(x+2)$

14. Solve by factoring: $3x^3 - 9x^2 = 30x$

$$\begin{aligned}3x^3 - 9x^2 - 30x &= 0 \\ 3x(x^2 - 3x - 10) &= 0 \\ 3x(x-5)(x+2) &= 0 \\ x=0/x=5/x=-2 &\quad \{0, 5, -2\}\end{aligned}$$

15. Factor and check: $8x^3 + 125$.

$$8x^3 + 125 = (2x+5)(4x^2 - 10x + 25)$$

$$\begin{aligned}\text{check } (2x+5)(4x^2 - 10x + 25) &= 8x^3 - 20x^2 + 50x + 20x^2 - 50x + 125 \\ &= 8x^3 + 125 \checkmark\end{aligned}$$

Sep 1-4:33 PM

Requiz by end of week

Thursday Quiz 2 (Days 4-9)

Monday Quiz 3 (Days 11-12)

Next Wednesday Test

Tues 9/24 1st Math League
Meeting in LGR 2:30pm

Sep 17-10:09 PM

1-11: Solve Quadratic Equations Using the Quadratic Formula

If we have a quadratic equation that is not easily factorable, we can solve it by using the quadratic formula. Try solving this by factoring: $3x^2 + 5x - 1 = 0$

What do you notice?

1, 3

$P = -3$
 $S = 5$

The Quadratic Formula

If $ax^2 + bx + c = 0$ ($a \neq 0$), then the solutions, or roots, are

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

<https://www.youtube.com/watch?v=2lbABbfU6Zc> (To music)

<http://www.youtube.com/watch?v=O8ezDEk3qCg>
<http://www.youtube.com/watch?v=z6hCu0EPs-o>

You should recognize the expression under the radical = $b^2 - 4ac$.

We call that the discriminant and will find it first.

Let's use the quadratic formula to solve the following equation. Find the discriminant first.

$$1. 3x^2 + 5x - 1 = 0 \quad a = 3, b = 5, c = -1$$

$$b^2 - 4ac = 5^2 - 4(3)(-1) = 25$$

$$25 + 12 = 37$$

$$x = \frac{-5 \pm \sqrt{37}}{2(3)} \Rightarrow \frac{-5 \pm \sqrt{37}}{6}$$

Aug 28-12:33 PM

Find the zeros of the functions or the roots of the equations using the quadratic formula. Leave all solutions in simplest radical form.

Note: Some can be solved by factoring, but we will use the quadratic formula.

$$2. f(x) = x^2 + 8x + 7$$

$$x^2 + 8x + 7 = 0$$

$$\text{discrim} = b^2 - 4ac = (8)^2 - 4(1)(7)$$

$$= 64 - 28 = 36$$

$$x = \frac{-8 \pm \sqrt{36}}{2(1)} = \frac{-8 \pm 6}{2}$$

$$\begin{array}{l|l} x = \frac{-8+6}{2} & x = \frac{-8-6}{2} \\ x = \frac{-2}{2} & x = \frac{-14}{2} \\ x = -1 & x = -7 \end{array} \quad \left\{ -1, -7 \right\}$$

$$3. -9 = x^2 + 6x$$

$$X$$

$$\begin{aligned} x^2 + 6x + 9 &= 0 \\ b^2 - 4ac &= \\ 36 - 4(1)(9) &= \\ &= 36 - 36 \end{aligned}$$

$$x = \frac{-6 \pm \sqrt{0}}{2(1)} = \frac{-6}{2} = 0$$

$$\{ -3 \}$$

Aug 28-12:39 PM

$$4. 3(x-2)^2 - 4 = 0$$

$$3[x^2 - 2x - 2x + 4] - 4 = 0 \quad x = \frac{-12 \pm \sqrt{48}}{2(3)}$$

$$3(x^2 - 4x + 4) - 4 = 0$$

$$3x^2 - 12x + 12 - 4 = 0 \quad x = 12 \pm \cancel{15}$$

$$3x^2 - 12x + 8 = 0$$

$$\begin{aligned} b^2 - 4ac &= 144 - 4(3)(8) \\ &= 144 - 96 \\ &= 48 \end{aligned}$$

$$a = 3, b = -12, c = 8$$

$$x = \frac{12 \pm \sqrt{48}}{6}$$

$$= \frac{12 \pm 4\sqrt{3}}{6} = \frac{12}{6} \pm \frac{4\sqrt{3}}{6}$$

$$\begin{aligned} &\div 2 = \frac{-6 \pm 2\sqrt{3}}{3} \\ &\quad \left\{ \frac{-6 \pm 2\sqrt{3}}{3} \right\} \end{aligned}$$

$$5. f(x) = 2x^2 - 16x + 27$$

Aug 28-12:40 PM

You can use the quadratic formula to solve real-world problems modeled by quadratic functions.

6. In a shot put event, Jenna tosses her last shot from a position of about 6' above the ground with an initial vertical and horizontal velocity of 20 ft/sec. The height of the shot is modeled by the function $h(t) = -16t^2 + 20t + 6$, where t is the time in seconds after the toss. How long does it take the shot to reach the ground? Round to the nearest tenth.

$$(-16t^2 + 20t + 6 = 0) - 1$$

~~$$\star \frac{16t^2 - 20t - 6}{2} = 0$$~~

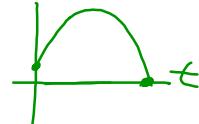
$$\text{discrim} = b^2 - 4ac$$

$$= (-20)^2$$

$$= 400 - 4(16)(-6)$$

$$= 400 + 384 = 784$$

$$8t^2 - 20t - 3 = 0$$



$$t = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$= \frac{(20 \pm \sqrt{784})}{32}$$

$$t = \frac{20 + \sqrt{784}}{32}$$

~~0.25~~
 1.5
 seconds

Aug 28-12:41 PM

Sep 20-6:28 PM