

Warm-Up:

Consider the system of equations below. Find the solution.

$$y = x^2 - 2x + 3$$

$$y = -x + 5$$

Sep 24-9:44 AM

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$$y_1 = x^2 - 2x + 3$$

$$y_2 = -x + 5$$

Algebraically

$$\begin{array}{r} -x + 5 = x^2 - 2x + 3 \\ +x - 5 \quad +x - 5 \end{array}$$

$$\begin{array}{r} x^2 - x - 2 = 0 \\ (x-2)(x+1) = 0 \end{array}$$

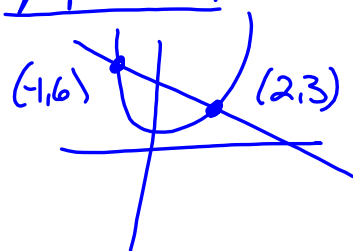
$$x = 2 \quad | \quad x = -1$$

$$\begin{array}{r|l} y = -2 + 5 & y = -(-1) + 5 \\ y = 3 & y = 6 \end{array}$$

$$\{(2, 3), (-1, 6)\}$$

OR

graphically



$$\{(2, 3), (-1, 6)\}$$

Sep 24-9:44 AM

The number i

Algebra 2 Unit 4 Day 1

On your own, solve each equation for x.

1. $x - 1 = 0$ $x = 1$

2. $x + 1 = 0$ $x = -1$

3. $x^2 - 1 = 0$ $\sqrt{x^2} = \pm 1$ $x = \pm 1$

4. $x^2 + 1 = 0$ $\sqrt{x^2} = \sqrt{-1}$ $x = \pm \sqrt{-1}$

5. $x^2 + 2 = 0$ $\sqrt{x^2} = \sqrt{-2}$ $x = \pm \sqrt{-2}$

$$\textcircled{4} \quad x^2 + 1 = 0$$

$$\sqrt{x^2} = \pm \sqrt{-1}$$

$$x = \pm i$$

nonreal answer

$$\textcircled{5} \quad \sqrt{x^2} = \pm \sqrt{-2}$$

$$x = \pm i\sqrt{2}$$

Which ones above do not have a real number solution? Why?

4 & 5, b/c we can't take the $\sqrt{}$ of a negative # in the real # system

Sep 1-1:53 PM

In fact, solving the equation $x^2 + 1 = 0$, we got $x = \pm \sqrt{-1}$.This leads to $i = \sqrt{-1}$.Problem: There is no real number that is the square root of a negative real number.Solution: The number i.We let $\sqrt{-1} = i$, then $i^2 = -1$.

$$(\sqrt{-1})^2 = -1$$

$$\sqrt{-1} \cdot \sqrt{-1} =$$

If $r > 0$, $\sqrt{-r} = \sqrt{-1} \cdot \sqrt{r} = i\sqrt{r}$ \mathbb{R} Definition: A pure imaginary number is a number that can be written in the form
 bi where $b \in \mathbb{R}$ and $i = \sqrt{-1}$
 $b \neq 0$

b is an element of the
real # system

Jun 30-9:40 AM

$$2x + 3x = 5x$$

$$2i + 3i = 5i$$

Rules of i:

1. Change all expressions of the form $\sqrt{-b}$ to $i\sqrt{b}$ first
2. Treat i as a variable for addition and subtraction.
3. Substitute -1 for i^2

$$\sqrt{x^2 \pm 9} \quad (\pm 9) \quad \sqrt{\quad} = + \sqrt{\quad}$$

Simplify:

1. $\sqrt{-9} = i\sqrt{9} = 3i$
2. $-\sqrt{-100} = -i\sqrt{100} = -10i$
3. $\sqrt{-20} = i\sqrt{4 \cdot 5} = 2i\sqrt{5}$
4. $2\sqrt{-27} = 2i\sqrt{9 \cdot 3} = 6i\sqrt{3}$

Sep 1-1:55 PM

Note: In the real number system $\sqrt{a} \cdot \sqrt{b} = \sqrt{a \cdot b}$. However, this is not the case when working with imaginary numbers.

Example: Simplify the following using: a) rules for real numbers, and then b) rules for i.

$$\begin{aligned} \text{a) } \sqrt{-4} \cdot \sqrt{-25} \\ = \sqrt{-4 \cdot -25} \\ = \sqrt{100} \\ = 10 \end{aligned}$$

$$\text{b) } \sqrt{-4} \cdot \sqrt{-25}$$

$$\begin{aligned} &= i\sqrt{4} \cdot i\sqrt{25} \\ &= 2i \cdot 5i \\ &= 10i^2 \\ &= 10(-1) = -10 \end{aligned}$$

$$i^2 = -1$$

What do you notice?

The answers are opposites

Simplify:

$$5. \sqrt{-9} \cdot \sqrt{-16} = i\sqrt{9} \cdot i\sqrt{16} = 3i \cdot 4i = 12i^2 = 12(-1) = -12$$

$$6. \sqrt{5} \cdot \sqrt{-10} = \sqrt{5} \cdot i\sqrt{10} = i\sqrt{50} = i\sqrt{25 \cdot 2} = 5i\sqrt{2}$$

$$7. -\sqrt{-6} \cdot \sqrt{15} = -i\sqrt{6} \cdot \sqrt{15} = -i\sqrt{90} = -i\sqrt{9 \cdot 10} = -3i\sqrt{10}$$

$$8. (\sqrt{-7})^2 = \sqrt{49} = 7$$

$$\begin{aligned} (i\sqrt{7})^2 &= i\sqrt{7} \cdot i\sqrt{7} = i^2\sqrt{49} = i^2 \cdot 7 = 7i^2 = 7(-1) = -7 \\ (7-7) &= -7 \end{aligned}$$

Sep 1-1:55 PM

