

### Homework 7-3

Do Warm-up #1 & 2 in notes (GOOD for Quiz!)

NOTE Tues 12/17: Today, reference angles were introduced, but we did not practice any with radian measures. As a result, tonight's HW 7-4: you should do 1ab, 2-8 a part only, 9 and 10.

I am posting completed notes with radian measure reference angles as an fyi. If we need more practice, I will pull these back up.

- |                 |  |
|-----------------|--|
| 1. $\pi/10$     | 10. $83.1^\circ$   |
| 2. $-3\pi$      | 11. $435.4^\circ$  |
| 3. $7\pi/18$    | 12. $-206.3^\circ$   |
| 4. $420^\circ$  | 13-15 see next slide   |
| 5. $-540^\circ$ | 16. minute hand: $360^\circ$ , $2\pi$<br>hour hand: $60^\circ$ , $\pi/3$ |
| 6. $105^\circ$  | 17. $\pi$  |
| 7. $1.71$ rad   | 18. $0, \pi$   |
| 8. $-3.46$ rad  | 19. $0, \pi$   |
| 9. $4.71$ rad   | 20. $\pi/2, 3\pi/2$  |

Aug 13-1:33 PM

Name: Key Algebra 2 Homework 7-3  
 Period: \_\_\_\_\_

State each angle in radians in terms of  $x$ .

- $18^\circ \left(\frac{\pi}{180}\right) = \frac{\pi}{10}$
- $-540^\circ \left(\frac{\pi}{180}\right) = -3\pi$
- $70^\circ \left(\frac{\pi}{180}\right) = \frac{7\pi}{18}$

Convert the radian measures to degrees, rounded to the nearest degree.

- $\frac{7\pi}{3} \left(\frac{180}{\pi}\right) = 420^\circ$
- $-3\pi \left(\frac{180}{\pi}\right) = -540^\circ$
- $\frac{7\pi}{12} \left(\frac{180}{\pi}\right) = 105^\circ$

State each angle to the nearest hundredth of a radian. Do not leave your answer in terms of  $x$ .

- $98^\circ \left(\frac{\pi}{180}\right) = 1.71$  rad  $\frac{98\pi}{180} =$
- $-198^\circ \left(\frac{\pi}{180}\right) = -3.46$  rad
- $270^\circ \left(\frac{\pi}{180}\right) = 4.71$  rad

Convert the radian measures to the nearest tenth of a degree.

- $1.45 \left(\frac{180}{\pi}\right) = 83.1^\circ$
- $7.6 \left(\frac{180}{\pi}\right) = 435.4^\circ$
- $-3.6 \left(\frac{180}{\pi}\right) = -206.3^\circ$

Sketch the following angles:

13.  $\frac{5\pi}{6}$

14.  $\frac{5\pi}{3}$

15.  $-\frac{7\pi}{4}$

16. A clock starts at midnight. It is now 2 AM. What angle has the minute hand swept through in one hour? What angle has the hour hand swept through in two hours? State both answers in degrees and radians. Hint: Pay special attention to the direction of rotation.

Minute hand =  $360^\circ$   
 =  $2\pi$  rad

Hour hand:  $\frac{2}{12} = \frac{x}{360}$   $\frac{2}{12} = \frac{x}{2\pi}$   
 $x = 60^\circ, \pi$   $x = \frac{\pi}{3}$  rad

Using the unit circle, find all of the measure of angle  $\theta$ .  $0 \leq \theta < 2\pi$

17.  $\cos(\theta) = -1$  (means what angle has a cosine = -1?)  $\pi$

18.  $\sin(\theta) = 0$   $(-, 0)$   $0, \pi$

19.  $\tan(\theta) = 0$   $0, \pi$

20.  $\tan(\theta) = \text{undefined}$   $\frac{\pi}{2}, \frac{3\pi}{2}$

$\tan \theta = \frac{\sin \theta}{\cos \theta}$

**Day 4: Reference Angles and ASTC**

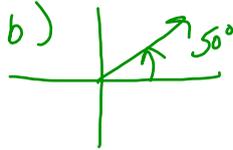
(7-3 notes)

Warm-Up:

- Convert the angle to radians or degrees.
- Sketch the angle in standard position, and determine the quadrant in which the angle lies.
- Find the measures of a positive and negative angle that are coterminal with the given angle.

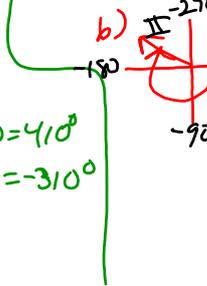
1.  $50^\circ$

a)  $50 \cdot \frac{\pi}{180} = \frac{50\pi}{180} = \frac{5\pi}{18}$



c)  $50 + 360 = 410^\circ$   
 $50 - 360 = -310^\circ$

2. a)  $\frac{-4\pi}{3} \cdot \frac{180}{\pi} = -240^\circ$



c)  $-240 + 360 = 120^\circ$   
 $-240 - 360 = -600^\circ$

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QUIZ

Dec 15-7:11 PM

**Sine, Cosine and Tangent in Quadrants:**

For a unit circle  $(x,y) = (\cos\theta, \sin\theta)$   
 $\tan\theta = \frac{\sin\theta}{\cos\theta}$

|   |   |   |   |
|---|---|---|---|
| <p>Quad I<br/> <math>(+,+)</math><br/> <math>\text{I}</math></p> <p><math>\sin(\theta) +</math><br/> <math>\cos(\theta) +</math><br/> <math>\tan(\theta) +</math></p> | <p>Quad II<br/> <math>(-,+)</math><br/> <math>\text{II}</math></p> <p><math>\sin(\theta) +</math><br/> <math>\cos(\theta) -</math><br/> <math>\tan(\theta) -</math></p> | <p>Quad III<br/> <math>(-,-)</math><br/> <math>\text{III}</math></p> <p><math>\sin(\theta) -</math><br/> <math>\cos(\theta) -</math><br/> <math>\tan(\theta) +</math></p> | <p>Quad IV<br/> <math>(+,-)</math><br/> <math>\text{IV}</math></p> <p><math>\sin(\theta) -</math><br/> <math>\cos(\theta) +</math><br/> <math>\tan(\theta) -</math></p> |
|---|---|---|---|

**SOH CAH TOA**

**Sine | All**  
**Tangent | Cosine**

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Determine the quadrant in which angle  $\theta$  may lie if:

|   |   |
|---|---|
| S | A |
| T | C |

a.  $\tan(\theta) < 0$  and  $\sin(\theta) = \frac{3}{5}$   
~~II, IV~~ **II, I, III**

b.  $\cos(\theta) = -1/2$  and  $\sin(\theta) < 0$   
~~II, III~~ **III, IV**

c.  $\tan(\theta) < 0$  and  $\cos(\theta) < 0$   
~~II, III~~ **II, III**  
**II**

d.  $\tan(\theta) > 0$  and  $\cos(\theta) = .6$   
~~I, III~~ **I, IV**  
**I**

Aug 13-11:47 AM

Definition: A reference angle is a positive and acute angle formed by the terminal side and the x-axis. It is often denoted by the symbol  $\alpha$  (alpha).

Note: Quadrants do not have reference angles.

Quad I:

Quad II:  $150^\circ$   
  
 $ref\ angle = 180 - \theta = 180 - 150 = 30^\circ$

Quad III:  $200^\circ$   
  
 $ref\ angle = \theta - 180 = 200 - 180 = 20^\circ$

Quad IV:  $300^\circ$   
  
 $ref\ angle = 360 - \theta = 360 - 300 = 60^\circ$

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Sketch and find the reference angle:

1.  $320^\circ$   
  
 $\alpha = 40^\circ$

2.  $275^\circ$   
  
 $\alpha = 360 - 275 = 85^\circ$

3.  $\frac{5\pi}{4}$   
  
 $\alpha = \frac{5\pi}{4} - \pi = \frac{\pi}{4}$

4.  $\frac{4\pi}{3}$   
  
 $\alpha = \frac{4\pi}{3} - \pi = \frac{\pi}{3}$

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5.  $\frac{\pi}{4}$

6.  $\frac{3\pi}{2}$   $\cdot \frac{180}{\pi}$

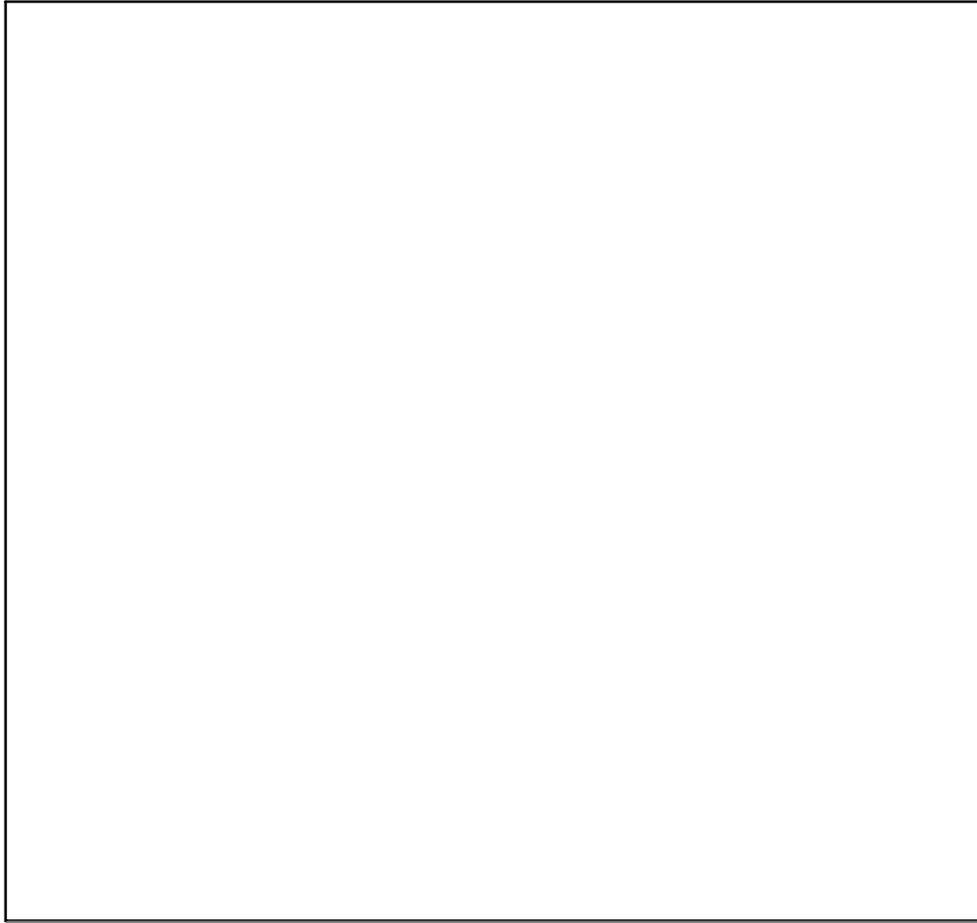
7.  $-\frac{5\pi}{6}$

8.  $-\frac{2\pi}{3}$

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9.  $-\frac{9\pi}{5}$

Dec 16-5:58 PM



Dec 16-5:50 PM