

Homework 7-4

Do warm-up at top of Day 5 notes and find the angle measure in degrees to the nearest tenth.

#1 - 8 a) see next slide for sketches

#1 - 8 b) reference angles:

1. 30° 2. $\pi/6$ 3. $\pi/3$ 4. None

5. 45° 6. $\pi/4$ 7. $\pi/6$ 8. $\pi/3$

9. III

10. D

Yesterday reference angles were introduced, but we did not practice any with radian measures. So for HW 7-4: you should have been able to do 1ab, 2-8 a part only, 9 and 10.

Completed notes were posted as an fyi.

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Name: Key Algebra 2 Homework 7-4
Period: _____

For #1 - 8:

a. Sketch the angle in standard position.
b. State the reference angle for each (if possible).

1. 150°

$\alpha = 30^\circ$
 $\alpha = 180 - 150 = 30^\circ$

2. $\frac{11\pi}{6}$

$\alpha = \frac{\pi}{6} (30^\circ)$
 $\alpha = \frac{12\pi}{6} - \frac{11\pi}{6} = \frac{\pi}{6}$

3. $\frac{4\pi}{3}$

$\alpha = \frac{\pi}{3} (60^\circ)$
 $\alpha = \frac{4\pi}{3} - \frac{3\pi}{3} = \frac{\pi}{3}$

4. 2π

$\alpha = \text{N/A}$

5. -135°

$\alpha = 45^\circ$
 $\alpha = 180 - 135 = 45^\circ$

6. $\frac{3\pi}{4}$

$\alpha = \frac{\pi}{4}$ (45°)
 $\alpha = \frac{4\pi}{4} - \frac{3\pi}{4} = \frac{\pi}{4}$

7. $-\frac{\pi}{6}$

$\alpha = \frac{\pi}{6}$ (30°)

8. $-\frac{4\pi}{3}$

$\alpha = \frac{\pi}{3}$ (60°)
 $\alpha = \frac{4\pi}{3} - \frac{3\pi}{3} = \frac{\pi}{3}$

9. What quadrant is angle θ in if $\sin(\theta) = -.5$ and $\cos(\theta) < 0$?

III $\sin(-)$ $\cos(-)$

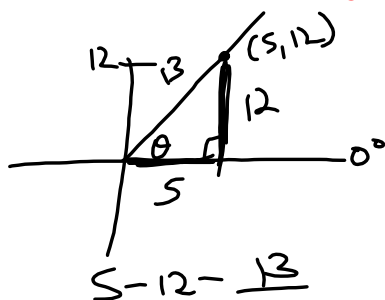
10. On the unit circle, the terminal side of an angle θ passes through the point $(a, -b)$. Both a and b are positive. Which is not true?

a. $\sin(\theta) = -b$ b. $\tan(\theta) < 0$ $\tan = \frac{y}{x} = \frac{-b}{a}$
 c. $\cos(\theta) = a$ d. $\frac{\sin(\theta)}{\cos(\theta)} > 0$

Warm-Up:

$P(5, 12)$ is a point on the terminal side of θ in standard position. Find the exact values of $\sin(\theta)$, $\cos(\theta)$, and $\tan(\theta)$.

Also find the measure of angle θ to the nearest tenth of a degree.



$$5^2 + 12^2 = c^2$$

$$169 = c^2$$

$$c = 13$$

$$\sin \theta = \frac{y}{r} = \frac{12}{13}$$

$$\cos \theta = \frac{x}{r} = \frac{5}{13}$$

$$\tan \theta = \frac{y}{x} = \frac{12}{5}$$

$$\theta = \sin^{-1}\left(\frac{12}{13}\right) \approx 67.4^\circ$$

Day 5 Goal:

Determine trig values in various quadrants given a point on a unit circle vs not on a unit circle.

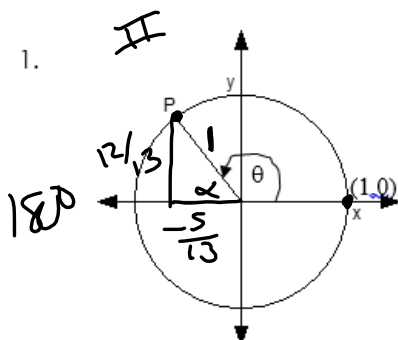
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Finding Trig Values Given a Point:

* Remember that if a point is on the unit circle, the x-coordinate = $\cos \theta$, the y-coordinate = $\sin \theta$, and $\tan(\theta) = \frac{\sin \theta}{\cos \theta}$. To find $\angle \theta$ we find the reference angle first using the positive lengths of the triangle sides, and then put that angle into the correct quadrant to find $\angle \theta$.

$$\tan \theta = \frac{\sin \theta}{\cos \theta}$$

Examples:



$$(\cos \theta, \sin \theta)$$

$$P\left(-\frac{5}{13}, \frac{12}{13}\right)$$

$$+\sin(\theta) = \frac{12}{13}$$

$$-\cos(\theta) = -\frac{5}{13}$$

$$-\tan(\theta) = \frac{12/13}{-5/13} = \frac{12}{13} \cdot -\frac{13}{5} = -\frac{12}{5}$$

$$m \angle \theta =$$

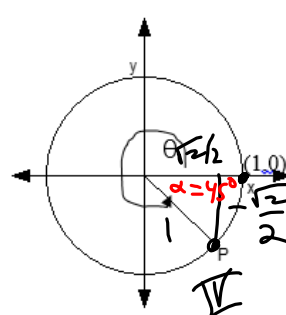
$$\alpha = \sin^{-1}\left(\frac{12}{13}\right) = 67^\circ$$

$$\theta = 180 - \alpha = 180 - 67^\circ = 113^\circ$$

$$\frac{S}{T} \mid \frac{A}{C}$$

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2.

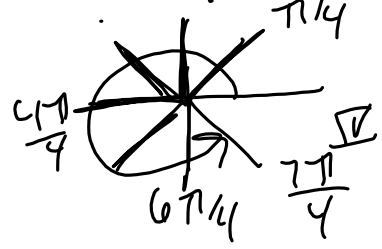


$(\cos \theta, \sin \theta)$
 $(+, -)$
 $P\left(\frac{\sqrt{2}}{2}, -\frac{\sqrt{2}}{2}\right)$

$\sin(\theta) = -\frac{\sqrt{2}}{2}$
 $\cos(\theta) = \frac{\sqrt{2}}{2}$
 $\tan(\theta) = \frac{-\frac{\sqrt{2}}{2}}{\frac{\sqrt{2}}{2}} = -1$

$m\angle\theta =$
 $\alpha = \cos^{-1}\left(\frac{\sqrt{2}}{2}\right) = 45^\circ$
 $\theta = 360^\circ - \alpha = 360^\circ - 45^\circ$
 $\theta = 315^\circ$
 radians $\rightarrow 315 \cdot \frac{\pi}{180} = \frac{315\pi}{180} = \frac{7\pi}{4}$

$\frac{S}{T} \mid \frac{A}{C}$


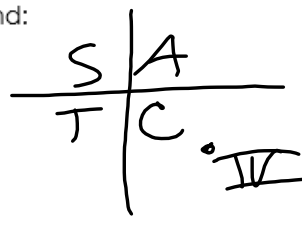


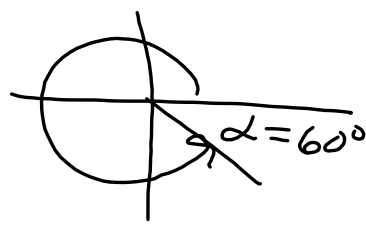
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3. Point $A\left(\frac{1}{2}, -\frac{\sqrt{3}}{2}\right)$ is on a unit circle with a center of the origin. If θ is an angle in standard position whose terminal side passes through A, find:

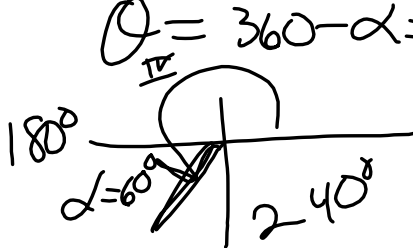
$(\cos \theta, \sin \theta) \rightarrow (+, -)$

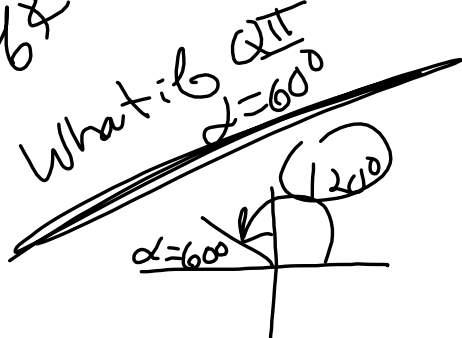
a. $\sin(\theta) = -\frac{\sqrt{3}}{2}$
 b. $\cos(\theta) = \frac{1}{2}$
 c. $\tan(\theta) = -\frac{\frac{\sqrt{3}}{2}}{\frac{1}{2}} = -\sqrt{3}$
 d. $m\angle\theta$
 $\alpha = \cos^{-1}\left(\frac{1}{2}\right) = 60^\circ$

$\frac{S}{T} \mid \frac{A}{C}$




$\theta = 360^\circ - \alpha = 300^\circ$



What if $\frac{QII}{\alpha = 60^\circ}$


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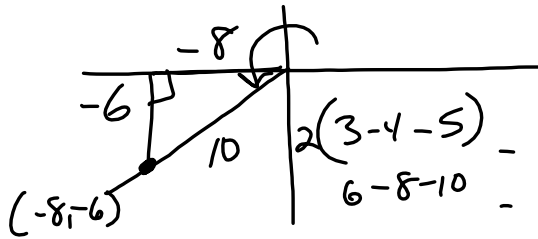
$(-, -)$

4. $P(-8, -6)$ is a point on the terminal side of θ in standard position. Find the exact values of $\sin(\theta)$, $\cos(\theta)$ and $\tan(\theta)$.

Why is this example different?

Not on a Unit circle

$$(x, y) \neq (\cos \theta, \sin \theta)$$



$$\begin{aligned} (-6)^2 + (-8)^2 &= c^2 \\ 100 &= c^2 \\ c &= 10 \end{aligned}$$

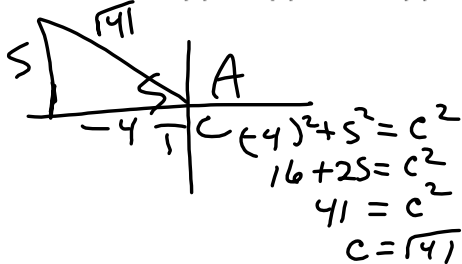
$$\textcircled{+} \tan \theta = \frac{-6}{-8} = \frac{3}{4}$$

$$\begin{aligned} \sin \theta &= \frac{-6}{10} = -\frac{3}{5} \\ \cos \theta &= \frac{-8}{10} = -\frac{4}{5} \end{aligned}$$

S/A
T/C

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5. $P(-4, 5)$ is a point on the terminal side of θ in standard position. Find the exact values of $\sin(\theta)$, $\cos(\theta)$ and $\tan(\theta)$.



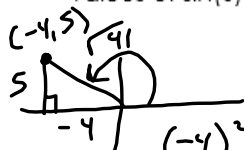
$$\begin{aligned} \textcircled{+} \sin \theta &= \frac{y}{r} = \frac{5}{\sqrt{41}} \cdot \frac{\sqrt{41}}{\sqrt{41}} = \frac{5\sqrt{41}}{41} \\ \cos \theta &= \frac{x}{r} = \frac{-4}{\sqrt{41}} \cdot \frac{\sqrt{41}}{\sqrt{41}} = \frac{-4\sqrt{41}}{41} \\ \tan \theta &= \frac{y}{x} = \frac{5}{-4} = -\frac{5}{4} \end{aligned}$$

6. $P(-2, -3)$ is a point on the terminal side of θ in standard position. Find the exact values of $\sin(\theta)$, $\cos(\theta)$ and $\tan(\theta)$.

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$$(-, +) = \text{II}$$

5. $P(-4, 5)$ is a point on the terminal side of θ in standard position. Find the exact values of $\sin(\theta)$, $\cos(\theta)$ and $\tan(\theta)$.

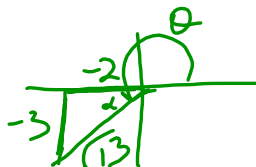


$$\begin{aligned} (-4)^2 + 5^2 &= c^2 \\ 16 + 25 &= c^2 \\ 41 &= c^2 \\ c &= \sqrt{41} \end{aligned}$$

$$\begin{aligned} \sin \theta &= \frac{5}{\sqrt{41}} \cdot \frac{\sqrt{41}}{\sqrt{41}} = \frac{5\sqrt{41}}{41} \\ \cos \theta &= \frac{-4}{\sqrt{41}} \cdot \frac{\sqrt{41}}{\sqrt{41}} = \frac{-4\sqrt{41}}{41} \\ \tan \theta &= -\frac{5}{4} \end{aligned}$$

$$(\sqrt{41})^2$$

6. $P(-2, -3)$ is a point on the terminal side of θ in standard position. Find the exact values of $\sin(\theta)$, $\cos(\theta)$ and $\tan(\theta)$.



$$\begin{aligned} (-2)^2 + (-3)^2 &= c^2 \\ 4 + 9 &= c^2 \\ 13 &= c^2 \\ c &= \sqrt{13} \end{aligned}$$

$$\begin{aligned} \sin \theta &= \frac{-3}{\sqrt{13}} \cdot \frac{\sqrt{13}}{\sqrt{13}} = \frac{-3\sqrt{13}}{13} \\ \cos \theta &= \frac{-2}{\sqrt{13}} \cdot \frac{\sqrt{13}}{\sqrt{13}} = \frac{-2\sqrt{13}}{13} \\ \tan \theta &= \frac{-3}{-2} = \frac{3}{2} \end{aligned}$$

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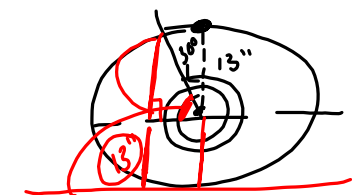
Application Word Problems:

1. A bicycle wheel with a radius of 13" has a valve cap positioned at the highest point of the wheel. If the wheel is spun 750° in one direction, how high is the valve cap above the ground? Round your answer to the nearest tenth of an inch.

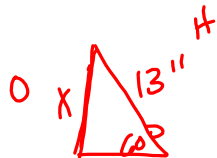
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Application Word Problems: $r = 13''$

1. A bicycle wheel with a radius of $13''$ has a valve cap positioned at the highest point of the wheel. If the wheel is spun 750° in one direction, how high is the valve cap above the ground? Round your answer to the nearest tenth of an inch.



600



$$\frac{\sin 60^\circ}{1} = \frac{x}{13}$$

$$x = 13 \sin 60^\circ = 11.258$$

$$\begin{array}{r} + 13 \\ \hline 24.258 \end{array}$$

$$\approx 24.3''$$

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