

Groups:

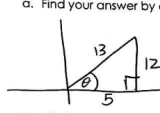
- Check your homework with each other.
- Try to come to consensus on the answers.
- When you do have me check.
- When you have all right....

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Name: Kuf Algebra 2 Homework 7-6
Period: _____

1. On a unit circle, $\sin(\theta) = \frac{12}{13}$ and θ is acute. What is the exact values of $\cos(\theta)$?

a. Find your answer by drawing the triangle in the correct quadrant in standard position.



$$\cos(\theta) = \frac{5}{13}$$

b. Find your answer using the Pythagorean Identity.

$$\sin^2(\theta) + \cos^2(\theta) = 1$$

$$\left(\frac{12}{13}\right)^2 + \cos^2(\theta) = 1$$

$$\frac{144}{169} + \cos^2(\theta) = \frac{169}{169}$$

$$\cos^2(\theta) = \frac{25}{169}$$

$$\cos(\theta) = \pm \frac{5}{13}$$

Q.I. $\cos(\theta) = \frac{5}{13}$

2. Using the identity $\sin^2(\theta) + \cos^2(\theta) = 1$, find the value of $\tan(\theta)$, to the nearest hundredth, if $\sin(\theta)$ is 0.7 and θ is in Quadrant II.

$$\sin^2(\theta) + \cos^2(\theta) = 1$$

$$(0.7)^2 + \cos^2(\theta) = 1$$

$$0.49 + \cos^2(\theta) = 1$$

$$\cos^2(\theta) = 0.51$$

$$\cos(\theta) = \pm 0.714$$

Q.II. $\cos(\theta) = -0.714$

$$\tan(\theta) = \frac{\sin(\theta)}{\cos(\theta)} = \frac{0.7}{-0.714}$$

$$\tan(\theta) = -0.98$$

3. a. If $\cos(\theta) = \frac{4}{5}$, what are two possible values for $\sin(\theta)$?



$$\sin(\theta) = \pm \frac{3}{5}$$

b. Why are there two possible values for $\sin(\theta)$?

depends on what quadrant θ is in

c. Find $m < \theta$ if $270^\circ < \theta < 360^\circ$ to nearest tenth.

$$\alpha = \sin^{-1}\left(\frac{3}{5}\right) = 36.9^\circ$$

Q.III $\theta = \alpha + 180^\circ = 36.9^\circ + 180^\circ = 216.9^\circ$

$$\sin^2 \theta + \cos^2 \theta = 1$$

4. If $\sin^2(32^\circ) + \cos^2(M) = 1$, then M equals

a. 32° b. 58° c. 68° d. 72°

5. Using the Pythagorean Identity, given $\cos(\theta) = -0.5$, and angle θ is in quadrant III, find $\sin(\theta)$ and $\tan(\theta)$ to the nearest tenth.

$$\sin^2 \theta + \cos^2 \theta = 1$$

$$\sin^2 \theta + (-0.5)^2 = 1$$

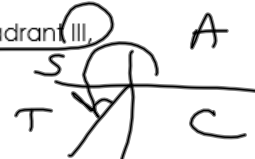
$$\sin^2 \theta = 1 - 0.25 = 0.75$$

$$\sqrt{\sin^2 \theta} = \sqrt{0.75}$$

$$\sin \theta = \pm 0.9$$

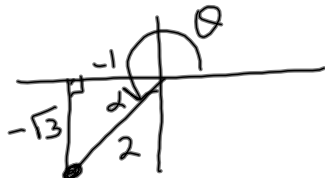
$$\text{III} \rightarrow \sin - , \sin \theta = -0.9$$

$$\tan \theta = \frac{\sin \theta}{\cos \theta} = \frac{-0.9}{-0.5} = 1.8$$



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6. Draw an angle in standard position given $\cos(\theta) = -1/2$, and angle θ is in quadrant III. Use the triangle to find $\sin(\theta)$ and $\tan(\theta)$ to the nearest tenth.



$$\sin \theta = \frac{O}{H} = \frac{-\sqrt{3}}{2} \approx -0.9$$

$$\tan \theta = \frac{-\sqrt{3}}{-1} = \sqrt{3} \approx 1.7$$

$$(-1, -\sqrt{3}) \quad (-1)^2 + b^2 = 2^2$$

$$b^2 = 4 - 1 = 3 \rightarrow b = \pm\sqrt{3}$$

7. Using the Pythagorean Identity, given $\sin(\theta) = -7/10$, and angle θ is in quadrant IV, find the exact values of $\cos(\theta)$ and $\tan(\theta)$.

$$\left(-\frac{7}{10}\right)^2 + \cos^2 \theta = 1$$

$$\cos^2 \theta = 1 - \frac{49}{100} = \frac{100}{100} - \frac{49}{100}$$

$$\sqrt{\cos^2 \theta} = \sqrt{\frac{51}{100}}$$

$$\cos \theta = \pm \frac{\sqrt{51}}{10}$$

$$\rightarrow \cos \theta = \frac{\sqrt{51}}{10}$$

$$\tan \theta = \frac{-7}{10} \cdot \frac{10}{\sqrt{51}}$$

$$\tan \theta = \frac{-7}{\sqrt{51}} = \frac{-7\sqrt{51}}{51}$$

8. If $\sin^2(\theta) + \cos^2(\pi) = 1$, then θ equals

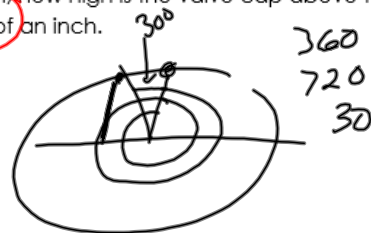
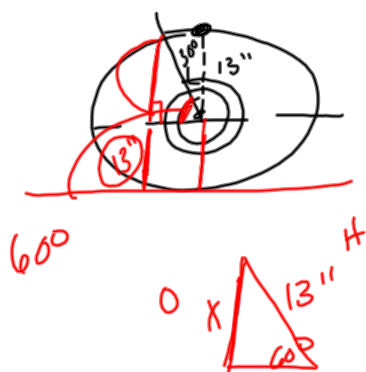
a. $-\theta$ b. $\pi/3$ c. π d. $\pi/2$



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Application Word Problems: $r = 13''$

1. A bicycle wheel with a radius of $13''$ has a valve cap positioned at the highest point of the wheel. If the wheel is spun 750° in one direction, how high is the valve cap above the ground? Round your answer to the nearest tenth of an inch.



$$\sin 60^\circ = \frac{x}{13}$$

$$x = 13 \sin 60^\circ = 11.258$$

$$\begin{array}{r} 11.258 \\ + 13 \\ \hline 24.258 \\ \approx 24.3'' \end{array}$$

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