

Name: \_\_\_\_\_ USKSHH 11/29/18 BC CAL

1) The graph of  $f(x) = \frac{x^2}{e^{2x}}$  has how many points of inflection?

A) 1      B) 2      C) 3      D) 4

$u=x^2$      $v=e^{-2x}$

$u'=2x$      $v'=-2e^{-2x}$

$u''=2$      $v''=4e^{-2x}$

2) What is the slope of the tangent to the graph of  $f(x) = \ln(\cos x)$  at  $x = -\frac{\pi}{3}$ ?

A)  $\sqrt{3}$     B)  $-\frac{\sqrt{3}}{3}$     C)  $-\frac{\sqrt{3}}{3}$     D)  $\frac{\sqrt{3}}{3}$

$u=\cos x$   
 $u'=-\sin x$   
 $u''=-\cos x$

$\frac{1}{4} = -\frac{-\sin x}{\cos x} = -\tan \frac{\pi}{3} = -\sqrt{3}$

3) The function,  $f(x) = \ln(x - x)$ , is increasing for

A)  $0 < x \leq e$     B)  $x \geq 1$     C)  $x > 0$     D)  $0 < x \leq 1$

$f'(x) = \frac{1}{x-1} - \frac{1}{x}$

4) If  $f(x) = xe^{-x}$ , then  $f'(1) =$

A)  $\frac{1}{e}$     B)  $2e^{-1}$     C) 0    D)  $e$

$u=x$      $v=e^{-x}$   
 $u'=1$      $v'=-e^{-x}$   
 $e^{-x}-xe^{-x} \rightarrow e^{-1}-1e^{-1} = \frac{1}{e}-\frac{1}{e}=0$

5) If  $f(x) = e^{\frac{1}{x}}$ , then  $f'(x) =$

A)  $e^{-\frac{1}{x^2}}$     B)  $e^{\frac{1}{x^2}}$     C)  $\frac{e^{\frac{1}{x}}}{x^2}$     D)  $-\frac{e^{\frac{1}{x}}}{x^2}$

$u=e^{-\frac{1}{x}}$   
 $u'=-\frac{1}{x^2}$

6) If  $f(x) = e^{\cos x}$ , then  $f'(x) =$

A)  $\cos x (\sin^2 x - \cos x)$     B)  $e^{\cos x} (\sin^2 x + \cos^2 x)$   
 $e^{\cos x} (-\sin x)$     C)  $e^{\cos x} (\cos x - \sin^2 x)$   
 $e^{\cos x} (\sin x - \cos x)$     D)  $-\sin x e^{\cos x}$

7) If  $f(x) = \sec^{-1}(x^2)$ , then  $f'(x) =$

A)  $\frac{2}{x\sqrt{x^2-1}}$     B)  $\frac{2x}{x^2+1}$     C)  $\frac{2x}{\sqrt{x^2-1}}$     D)  $\frac{2}{x(x^2-1)}$

$u=x^2$   
 $u'=2x$

$\frac{2x}{x^2\sqrt{x^2-1}} = \frac{2}{x\sqrt{x^2-1}}$

15) Find  $\frac{dy}{dx}$  for the given function

$y = \cos^{-1}(3x^2)$

$u=3x^2$   
 $u'=6x$

$\frac{-6x}{\sqrt{1-9x^4}} = \frac{-6x}{\sqrt{1-9x^4}}$

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Questions 7 through 9 refer to the following:  
 Find the derivative of the given function.

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7)  $g(x) = e^{-\frac{1}{x^2}}$

$u=-x^2$   
 $u'=2x^{-3}$   
 $\frac{2e^{-\frac{1}{x^2}}}{x^3}$

8)  $y = (\ln x)^2 \left(\frac{1}{x}\right)$

$3(\ln x)^2 \left(\frac{1}{x}\right) \frac{3 \ln^2 x}{x}$

9)  $f(x) = \ln |\sin x|$

$u=\sin x$      $\frac{\cos x}{\sin x} = +\tan x$

10)  $\frac{d}{dx} [s^{(x^2+1)}] =$

A)  $(2x)s^{(x^2+1)}$     B)  $(x^2+1)s^{x^2}$     C)  $s^{(x^2+1)} \ln 5$     D)  $2x(s^{(x^2+1)})$

11) If  $y = 2^x$ , then  $\frac{dy}{dx} =$

A)  $2^x \ln 2$     B)  $2^{x-1}$     C)  $\frac{\ln 2}{2^x}$     D)  $x(2^{(x-1)})$

$u=2^x$   
 $u'=2^x \ln 2$

$2^x \ln 2 - 1$

12)  $\frac{d}{dx} [\operatorname{Arc tan} \frac{x}{2}] =$

A)  $\frac{1}{2+x^2}$     B)  $\frac{4}{4+x^2}$     C)  $\frac{2}{4+x^2}$     D)  $\frac{2}{x^2+4}$

$u=\frac{x}{2}$   
 $u'=\frac{1}{2}$

$\frac{1}{2+\frac{x^2}{4}} = \frac{2}{4+x^2}$

13) If  $y = \operatorname{Arc cos} \left(\frac{2x}{3}\right)$ , then  $\frac{dy}{dx} =$

A)  $-\frac{1}{3\sqrt{9-4x^2}}$     B)  $\frac{2}{\sqrt{9-4x^2}}$     C)  $\frac{2}{\sqrt{4x^2-9}}$     D)  $-\frac{2}{9\sqrt{9-4x^2}}$

$u=\frac{2x}{3}$   
 $u'=\frac{2}{3}$

$\frac{2}{3\sqrt{1-\frac{4x^2}{9}}} = \frac{2}{3\sqrt{1-\frac{4x^2}{9}}} = \frac{2}{\sqrt{9-4x^2}}$

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