

Given the parent function and a description of the transformation, write the equation of the transformed function,  $f(x)$ .

1. linear  $\rightarrow$  vertical stretch of 4, left 5 and down 2

$$f(x) = 4(x+5) - 2$$

2. cubic  $\rightarrow$   $r_{x\text{-axis}}$ , left 1, and up 2

$$f(x) = -((x+1)^3 + 2)$$

3. square root  $\rightarrow$  vertical compression of  $\frac{1}{2}$ , right 3, and up 4

$$f(x) = \frac{1}{2}\sqrt{x-3} + 4$$

4. quadratic  $\rightarrow$   $r_{x\text{-axis}}$ , vertical stretch of 2, left 3, and down 1

$$f(x) = -2(x+3)^2 - 1$$

Nov 28-12:24 PM

Dec 12-12:58 PM

Give the name of the parent function and describe the transformation (read left to right)

5.  $h(x) = 4\sqrt{x-5}$

Parent:  $P(x) = \sqrt{x}$

Transformation(s):

Vertical stretch 4  
right 5

6.  $g(x) = 2|x-3| + 1$

Parent:  $P(x) = |x|$

Transformation(s):

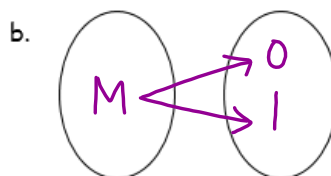
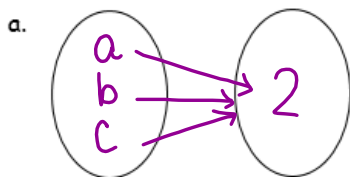
Vertical stretch 2  
right 3  
up 1

Nov 28-12:24 PM

7. Given the mapping diagram:

- write members of the domain and range and connect them with arrows so that  $f$  is a function and  $f^{-1}$  is not a function.
- write members of the domain and range so that  $f$  is not a function and  $f^{-1}$  is a function.

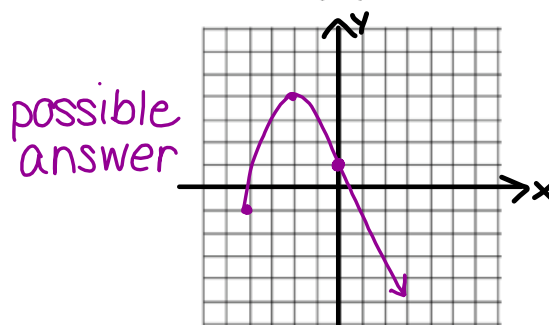
examples



Nov 28-12:24 PM

8. On the accompanying graph, draw a function that has the following properties:

- a. Domain:  $[-4, \infty]$
- b. Range:  $[-\infty, 4]$
- c. y-intercept:  $(0, 1)$
- d. as  $x \rightarrow \infty$ ,  $y \rightarrow -\infty$



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9. Given  $f(x) = 2x - 3$  and  $g(x) = -x + 4$ , perform the operation or composition. State domain restrictions if they exist.

$$\begin{aligned} \text{a. } f(g(x)) &= f(-x+4) \\ &= 2(-x+4) - 3 \\ &= -2x + 8 - 3 \end{aligned}$$

$$f(g(x)) = -2x + 5$$

$$\begin{aligned} \text{c. } g(x) - f(x) &= (-x+4) - (2x-3) \\ &= -x+4-2x+3 \\ &= -3x+7 \end{aligned}$$

$$\begin{aligned} \text{b. } f(x) \cdot g(x) &= (2x-3)(-x+4) \\ &= -2x^2 + 8x + 3x - 12 \\ &= -2x^2 + 11x - 12 \end{aligned}$$

$$\begin{aligned} \text{d. } \left( \frac{g}{f} \right)(x) &= \frac{g(x)}{f(x)} \\ &= \frac{-x+4}{2x-3} \quad x \neq \frac{3}{2} \end{aligned}$$

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## Review Race

- \* There are 7 rounds
- \* You may divide the questions in any way you wish
- \* Answers go on answer sheet
- \* Raise your hand when done
- \* Everyone must participate in every round -  
if you don't "play" - you don't win a prize
- \* 1st done - 3 points, 2nd - 2, 3rd - 1  
(with correct answers of course)
- \* Submit 3 wrong answers in a round? You are disqualified for that round!

Feb 24-8:01 AM

Functions  $f$ ,  $g$ , and  $h$  are given below. **Round 1**

$f(x) = x^3$   
 $f(0) = 0$   
 $g(x) = f(x) + 1$   
 $g(f(0)) = 0 + 1$

1. Find  $h(2) = -20$

2. Find  $g(f(0)) = 1$

3. Which statement is true about functions  $f$ ,  $g$ , &  $h$ ?  
(hint: look at graphs for  $f$  &  $g$  on your calculator)

- $f(x)$  and  $g(x)$  are odd,  $h(x)$  is even
- $f(x)$  and  $g(x)$  are even,  $h(x)$  is odd
- ☒  $f(x)$  is odd,  $g(x)$  is neither,  $h(x)$  is even
- $f(x)$  is even,  $g(x)$  is neither,  $h(x)$  is odd

4. Write an equation for  $k(x)$ , the transformation of  $f(x)$  translated right 2 and up 3  
**see below (from Group work)**  $k(x) = (x-2)^3 + 3$

5. Find the domain and range for  $h(x)$   
 $D: (-\infty, \infty)$   
 $R: [-20, \infty)$

④ from review sheet:  
 $x$ -axis up 1 :  $k(x) = -x^3 + 1$

Dec 1-10:07 AM

Given the function  $f(x) = (x - 3)^3 + 1$ ,

1. find  $f^{-1}(x)$ .

$$x = (y - 3)^3 + 1 \quad \rightarrow \quad y - 3 = \sqrt[3]{x - 1}$$

$$x - 1 = (y - 3)^3 \quad \rightarrow \quad y = \sqrt[3]{x - 1} + 3$$

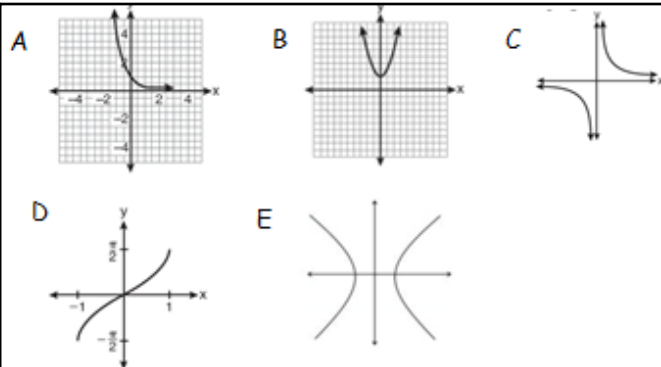
Round 2

2. what is the parent function and what transformation has occurred to produce  $f(x)$ ?

$$f^{-1}(x) = \sqrt[3]{x - 1} + 3$$

$P(x) = x^3 \rightarrow$  cubic  
right 3  
up 1

Dec 1-10:08 AM



Round 3

1. Which of the above graphs are not functions?

E

2. Which of the graphs are 1 - 1 functions?

A, C, D

3. Which of the graphs are even?

B, E

4. Which of the graphs are odd?

C, E, D

5. What is the domain and range for graph D?

$$D: [-1, 1]$$

$$R: \left[-\frac{\pi}{2}, \frac{\pi}{2}\right]$$

Dec 1-10:08 AM

Given:

$$f(x) = x^2 - 2x, g(x) = \sqrt{x+1}, \text{ and } k(x) = x - 2$$

Round 4

Find each of the following (state any restrictions where they exist):

1.  $f(n+1) = n^2 - 1$

2.  $g(f(4)) = 3$

3.  $f(g(x)) = x + 1 - 2\sqrt{x+1}$   
 $x \geq -1$

4.  $\left(\frac{f}{k}\right)(x) = x, x \neq 2$

5.  $(f+k)(x) = x^2 - x - 2$

6.  $(f-k)(x) = x^2 - 3x + 2$

④  $\frac{f(x)}{k(x)} = \frac{x(x-2)}{x-2} = x$

⑤  $f(x) + k(x) = x^2 - 2x + x - 2$   
 $= x^2 - x - 2$

⑥  $f(x) - k(x) = x^2 - 2x - x + 2$   
 $= x^2 - 3x + 2$

①  $f(n+1) = (n+1)^2 - 2(n+1)$   
 $= n^2 + 2n + 1 - 2n - 2$   
 $= n^2 - 1$

②  $g(f(4)) =$   
 $f(4) = 4^2 - 2(4) = 8$   
 $g(8) = \sqrt{8+1} = 3$

③  $f(g(x)) = f(\sqrt{x+1})$   
 $= (\sqrt{x+1})^2 - 2\sqrt{x+1}$   
 $= x + 1 - 2\sqrt{x+1}$

Dec 1-10:08 AM

1. Draw a function that is even

any graph symmetrical w.r.t. x-axis

2. Draw a function that is odd

any graph that looks the same upside down

3. Draw a function that is 1-1

any graph that passes vertical &amp; horizontal line tests

4. Draw a function that is not 1-1

passes vertical not horizontal

5. Draw a relation that is not a function but has an

inverse that is a function.

fails vertical passes horizontal

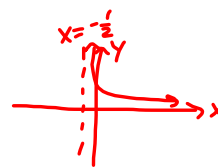
Round 5

Dec 1-10:08 AM

For each of the following,

- State the type of trouble.
- Find the domain algebraically.
- Sketch the graph.
- Use the graph to find the range.

1.  $f(x) = \frac{2}{\sqrt{2x+1}}$  **Double Trouble**  
 $2x+1 > 0$   
 $D: \{x | x > -\frac{1}{2}\}$   $R: \{y | y > 0\}$



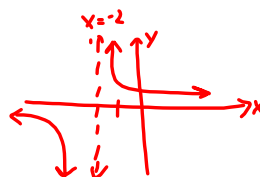
2.  $g(x) = x^2 + 1$  **NO Trouble**  $D: \{x | x \in \mathbb{R}\}$   
 $R: \{y | y \geq 1\}$



3.  $h(x) = \sqrt{2x+1}$  **Var Under sqrt**  
 $2x+1 \geq 0$   
 $D: \{x | x \geq -\frac{1}{2}\}$   $R: \{y | y \geq 0\}$



4.  $j(x) = \frac{1}{2x+4}$  **Var in denominator**  
 $2x+4 = 0$   
 $x = -2$   
 $D: \{x | x \neq -2\}$   $R: \{y | y \neq 0\}$



Dec 1-10:08 AM

Find the inverse algebraically and graphically.

**Round 7**

$f(x) = 3x - 2$

$x = 3y - 2$

$3y = x + 2$

$y = \frac{x+2}{3}$

$f^{-1}(x) = \frac{x+2}{3}$

**Graphically**

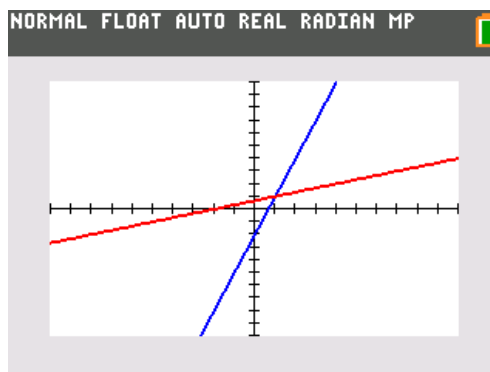
$f(x) \rightarrow$

x	-1	0	1	2
y	-5	-2	1	4

$f^{-1}(x) \rightarrow$

x	-5	-2	1	4
y	-1	0	1	2

Switch



Dec 1-10:09 AM

One free multiple  
choice answer on  
tomorrow's test

Prizes

You may ask one  
yes/no question on  
tomorrow's test



You will receive  
3 bonus points on  
tomorrow's test



Feb 24-8:07 AM

Dec 1-10:06 AM