

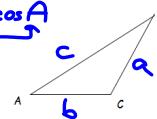
Turn in Graded HW with work stapled to the back

QUIZ

The Law of Cosines (SAS) Side-Included Angle-Side

The Law of Cosines is commonly used to solve oblique triangles and forms the basis for important trigonometric applications. When two sides of a triangle and the included angle are known, the law of cosines can be used to find the third side.

Law of Cosines: $a^2 = b^2 + c^2 - 2bc \cos A$



*Degree Mode

For each problem, draw a diagram and solve:

1. In $\triangle ABC$, $a = 3$, $b = 8$, and $\cos C = \frac{1}{4}$. Find c to the nearest integer.

$$\begin{aligned} &\text{SAS} \quad \begin{array}{c} \triangle ABC \\ \text{SAS} \end{array} \quad \begin{array}{l} \cos C = \frac{1}{4} \\ c^2 = 8^2 + 3^2 - 2(8)(3)(\frac{1}{4}) \\ c^2 = 61 \\ c = \sqrt{61} \approx 8 \end{array} \end{aligned}$$

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2. In $\triangle ABC$, $b = 4$, $c = 3$, $\angle A = 120^\circ$. Find a to the nearest integer.

$$\begin{array}{c} \triangle ABC \\ \text{SAS} \end{array} \quad \begin{array}{l} a^2 = 4^2 + 3^2 - 2(4)(3)\cos 120^\circ \\ a^2 = 37 \\ a = \sqrt{37} \approx 6 \end{array}$$

3. In $\triangle DEF$, $f = 12$, $d = 19$, $\angle E = 145^\circ$. Find e to the nearest integer.

$$\begin{array}{c} \triangle DEF \\ \text{SAS} \end{array} \quad \begin{array}{l} e^2 = 12^2 + 19^2 - 2(12)(19)\cos 145^\circ \\ e^2 = 64.196 \\ e = \sqrt{64.196} \approx 8 \end{array}$$

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4. In $\triangle QRS$, $q = 5$, $s = 8$, and $\cos R = \frac{2}{3}$. Find r to the nearest integer.

$$\begin{array}{c} \triangle QRS \\ \text{SAS} \end{array} \quad \begin{array}{l} r^2 = 8^2 + 5^2 - 2(8)(5)(\frac{2}{3}) \\ r^2 = 35.7 \\ r = \sqrt{35.7} \approx 6 \end{array}$$

5. In a parallelogram, two sides that are 20 cm and 12 cm long include an angle of 40° . Find the length (to the nearest centimeter) of the shorter diagonal of the parallelogram.

$$\begin{array}{c} \text{parallelogram} \\ \text{SAS} \end{array} \quad \begin{array}{l} x^2 = 12^2 + 20^2 - 2(12)(20)\cos 40^\circ \\ x^2 = 176.3 \\ x = 13 \text{ cm} \end{array}$$

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The Law of Cosines (SSS)

$$c^2 = a^2 + b^2 - 2ab \cos C$$

To find an angle of a triangle that does not contain a right angle where C is the angle opposite the side that you're looking for.

Draw a diagram and solve.

1. In $\triangle ABC$, $a = 10$, $b = 13$, and $c = 12$. Find $m\angle C$ to the nearest minute.
- $$\begin{array}{c} \triangle ABC \\ \text{SSS} \end{array} \quad \begin{array}{l} 12^2 = 13^2 + 10^2 - 2(13)(10)\cos C \\ \cos C = \frac{12^2 - 13^2 - 10^2}{-2(13)(10)} \\ \cos^{-1}\left(\frac{12^2 - 13^2 - 10^2}{-2(13)(10)}\right) \\ : 61^\circ 15' 51'' \quad \begin{array}{l} 30 \text{ seconds} \uparrow \\ \text{round up} \end{array} \\ = 61^\circ 16' \end{array}$$

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