

HW 5-1

1. $a^2 = b^2 + c^2 - 2bc\cos A$
2. 3
3. 3
4. $\sqrt{63} \approx 8$ $3\sqrt{7}$
5. 7
6. 14
7. $76^\circ 39'$

The Law of Cosines (SSS)

PreCalc Ch 5 Day 2

Warm-up: The lengths of 2 adjacent sides of a parallelogram ABCD are 16 cm and 20 cm. Find the length of the longer diagonal to the nearest cm, if the angle between the two sides is 35° . Draw a diagram and solve.

$$x^2 = 16^2 + 20^2 - 2(16)(20)\cos 145^\circ$$

$$\sqrt{x^2} = \sqrt{1180.26}$$

$$x = 34 \text{ cm}$$

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To find an angle of a triangle that does not contain a right angle:

 $c^2 = a^2 + b^2 - 2ab\cos C$ where C is the angle opposite the side that you need.

For each problem, draw a diagram and solve.

1. In $\triangle ABC$, $a = 8$, $b = 13$, and $c = 17$. Find $m\angle A$ to the nearest 10 minutes. $\rightarrow 2^{\text{nd}} \rightarrow \text{Apps} \rightarrow 4$

$$\text{Standard Rounding}$$

$$\cos A: \frac{8^2 + 17^2 - 13^2}{-2(8)(17)} = 1^\circ = 60'$$

$$\triangle A: \cos^{-1}\left(\frac{8^2 + 17^2 - 13^2}{-2(8)(17)}\right) = 26^\circ 57'$$
2. In $\triangle PQR$, $s = 21$, $t = 32$, and $u = 16$. Find the measure of $\angle S$ to the nearest minute. $\rightarrow 2^{\text{nd}} \rightarrow \text{Apps} \rightarrow 4$

$$32^2 = 16^2 + 21^2 - 2(16)(21)\cos S$$

$$\triangle S: \cos^{-1}\left(\frac{16^2 + 21^2 - 32^2}{-2(16)(21)}\right) = 119^\circ 7'$$

3. In
- $\triangle ABC$
- ,
- $a = 5$
- ,
- $b = 7$
- ,
- $c = 10$
- , find
- $\cos B$
- as a fraction in lowest terms.

$$7^2 = 10^2 + 5^2 - 2(10)(5)\cos B$$

$$\cos B = \frac{7^2 + 5^2 - 10^2}{-2(10)(5)}$$

$$\cos B = \frac{19}{5}$$

4. Jed is working on a stained glass project and needs to form a triangle with sides of 8, 12, and 15 inches out of lead cane to enclose the glass. To the nearest tenth of a degree, what is the largest angle he needs to create using the lead cane?

$$15^2 = 8^2 + 12^2 - 2(8)(12)\cos X$$

$$\triangle X: \cos^{-1}\left(\frac{8^2 + 12^2 - 15^2}{-2(8)(12)}\right) = 95.1^\circ$$

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Finding the Area of a Triangle (SAS)

$$\text{Area of a Triangle} = \frac{1}{2}ab\sin C$$

Side
Included Angle
Side

For each problem, draw a diagram and solve:

1. In
- $\triangle ABC$
- ,
- $m\angle A = 150^\circ$
- ,
- $b = 8$
- , and
- $c = 10$
- . Find the area of
- $\triangle ABC$
- .

$$K = \frac{1}{2}(8)(10)\sin 150^\circ$$

$$= 20 \text{ sq units}$$

2. In parallelogram ABCD,
- $AB = 20$
- ,
- $AD = 10$
- , and
- $m\angle A = 45^\circ$
- . Find the area of the parallelogram, rounded to the nearest tenth.

$$K = [\frac{1}{2}ab\sin C]2$$

$$= ab\sin C$$

$$= 10 \cdot 20 \sin 45^\circ$$

$$= 141.4 \text{ units}^2$$

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