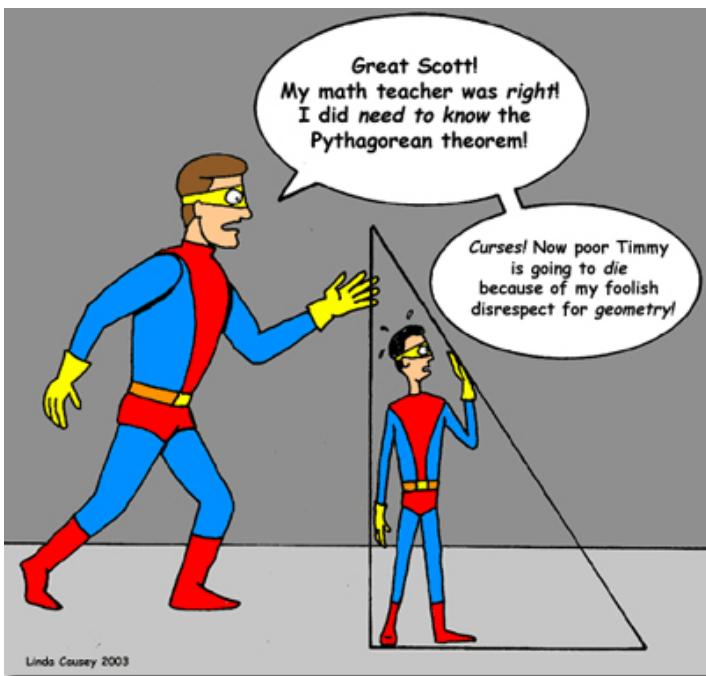


Addition & Subtraction Identities



Please change tonight's homework assignment to be Worksheet 7A All

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Addition & Subtraction Identities

PreCalc
Unit 7 Day 1

$$\sin(x + y) = \sin x \cos y + \cos x \sin y$$

$$\tan(x + y) = \frac{\tan x + \tan y}{1 - \tan x \tan y}$$

$$\sin(x - y) = \sin x \cos y - \cos x \sin y$$

$$\cos(x + y) = \cos x \cos y - \sin x \sin y$$

$$\cos(x - y) = \cos x \cos y + \sin x \sin y$$

$$\tan(x - y) = \frac{\tan x - \tan y}{1 + \tan x \tan y}$$



You must have these memorized !!!

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Simplify each using the formula:

$$\cos(x-y) = \cos x \cos y + \sin x \sin y$$

$$1. \cos(\pi - x)$$

$$= \cos \pi \cdot \cos x + \sin \pi \cdot \sin x$$

$$= -1 \cdot \cos x + 0 \cdot \sin x = -\cos x$$

$$2. \sin\left(\frac{\pi}{2} - \beta\right)$$

$$\sin(x-y) = \sin x \cos y - \cos x \sin y$$

$$= \sin \pi \cdot \cos \beta - \cos \pi \cdot \sin \beta$$

$$= 1 \cdot \cos \beta - 0 \cdot \sin \beta$$

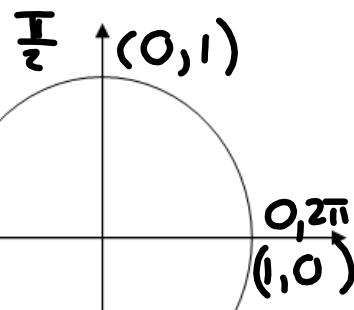
$$3. \sin(\pi + \alpha) : \cos \beta$$

$$= \sin \pi \cos \alpha + \cos \pi \sin \alpha$$

$$= \sin \pi \cos \alpha + \cos \pi \sin \alpha$$

$$= 0 \cdot \cos \alpha + (-1) \sin \alpha$$

$$= -\sin \alpha$$



| | $\frac{\pi}{6}$ | $\frac{\pi}{4}$ | $\frac{\pi}{3}$ | $\frac{2\pi}{3}$ |
|-----|----------------------|----------------------|----------------------|----------------------|
| sin | $\frac{1}{2}$ | $\frac{\sqrt{2}}{2}$ | $\frac{\sqrt{3}}{2}$ | $\frac{\sqrt{3}}{2}$ |
| cos | $\frac{\sqrt{3}}{2}$ | $\frac{\sqrt{2}}{2}$ | $\frac{1}{2}$ | $-\frac{1}{2}$ |
| tan | $\frac{\sqrt{3}}{3}$ | 1 | $\sqrt{3}$ | $-\sqrt{3}$ |

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Rewrite as a trigonometric function of a single angle, then evaluate:

$$4. \cos\left(\frac{7\pi}{18}\right) \cos\left(\frac{2\pi}{9}\right) + \sin\left(\frac{7\pi}{18}\right) \sin\left(\frac{2\pi}{9}\right) \quad \text{cos}(x-y) \quad \text{Change sign in #4}$$

$$: \cos\left(\frac{\pi}{4} - \frac{\pi}{9}\right) : \cos\left(\frac{7\pi}{18} - \frac{2\pi}{9}\right) : \cos\left(-\frac{3\pi}{18}\right) = \cos\frac{\pi}{6} \cdot \frac{\sqrt{3}}{2}$$

$$5. \frac{\tan\left(\frac{5\pi}{9}\right) + \tan\left(\frac{\pi}{9}\right)}{1 - \tan\left(\frac{5\pi}{9}\right) \tan\left(\frac{\pi}{9}\right)} : \tan\left(\frac{5\pi}{9} + \frac{\pi}{9}\right) : \tan\left(\frac{6\pi}{9}\right) = \tan\frac{2\pi}{3}$$

$$: -\sqrt{3}$$

$$6. \sin\left(\frac{2\pi}{3}\right) \cos\left(\frac{\pi}{6}\right) - \cos\left(-\frac{2\pi}{3}\right) \sin\left(\frac{\pi}{6}\right) \quad \text{Change } 10\pi/9 \text{ to } 2\pi/3$$

$$\sin(x-y)$$

$$: \sin\left(\frac{2\pi}{3} - \frac{\pi}{6}\right) : \sin\left(\frac{4\pi}{6} - \frac{\pi}{6}\right) : \sin\left(\frac{3\pi}{6}\right) = \sin\frac{\pi}{2} : 1$$

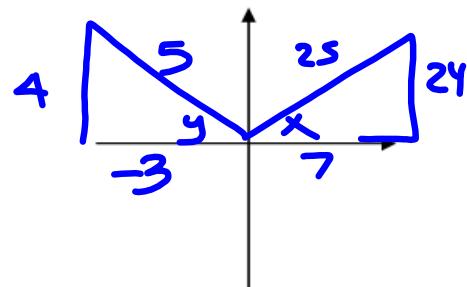
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7. Find the exact values of the following if x is in quadrant I and y is in quadrant II, $\sin x = \frac{24}{25}$ and

$$\sin y = \frac{4}{5}$$

a) $\sin(x+y)$

$$\begin{aligned} & \sin x \cos y + \cos x \sin y \\ & : \left(\frac{24}{25}\right)\left(-\frac{3}{5}\right) + \left(\frac{7}{25}\right)\left(\frac{4}{5}\right) \\ & : \frac{-72}{125} + \frac{28}{125} : -\frac{44}{125} \end{aligned}$$



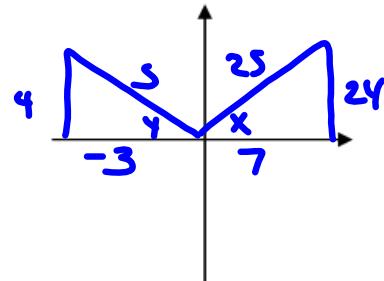
b) $\sin(x-y)$

$$\begin{aligned} & \sin x \cos y - \cos x \sin y \\ & : \left(\frac{24}{25}\right)\left(-\frac{3}{5}\right) - \left(\frac{7}{25}\right)\left(\frac{4}{5}\right) \\ & : -\frac{72}{125} - \frac{28}{125} : -\frac{100}{125} : -\frac{4}{5} \end{aligned}$$

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c) $\cos(x+y)$

$$\begin{aligned} & \cos x \cos y - \sin x \sin y \\ & : \left(\frac{7}{25}\right)\left(-\frac{3}{5}\right) - \left(\frac{24}{25}\right)\left(\frac{4}{5}\right) \\ & : -\frac{21}{125} - \frac{96}{125} : -\frac{117}{125} \end{aligned}$$

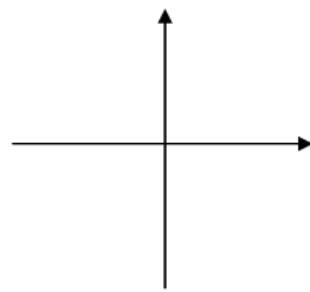


d) $\cos(x-y)$

$$\begin{aligned} & \cos x \cos y + \sin x \sin y \\ & : \left(\frac{7}{25}\right)\left(-\frac{3}{5}\right) + \left(\frac{24}{25}\right)\left(\frac{4}{5}\right) \\ & : -\frac{21}{125} + \frac{96}{125} : \frac{75}{125} : \frac{3}{5} \end{aligned}$$

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$$\begin{aligned}
 e) \tan(x+y) &:= \frac{\tan x + \tan y}{1 - \tan x \tan y} \\
 &\stackrel{7.3}{=} \frac{\left(\frac{24}{7}\right) + \left(-\frac{4}{3}\right)}{1 - \left(\frac{24}{7}\right)\left(-\frac{4}{3}\right)} \\
 &\stackrel{7.3}{=} \frac{72 + -28}{21 + 96} : \frac{44}{117}
 \end{aligned}$$



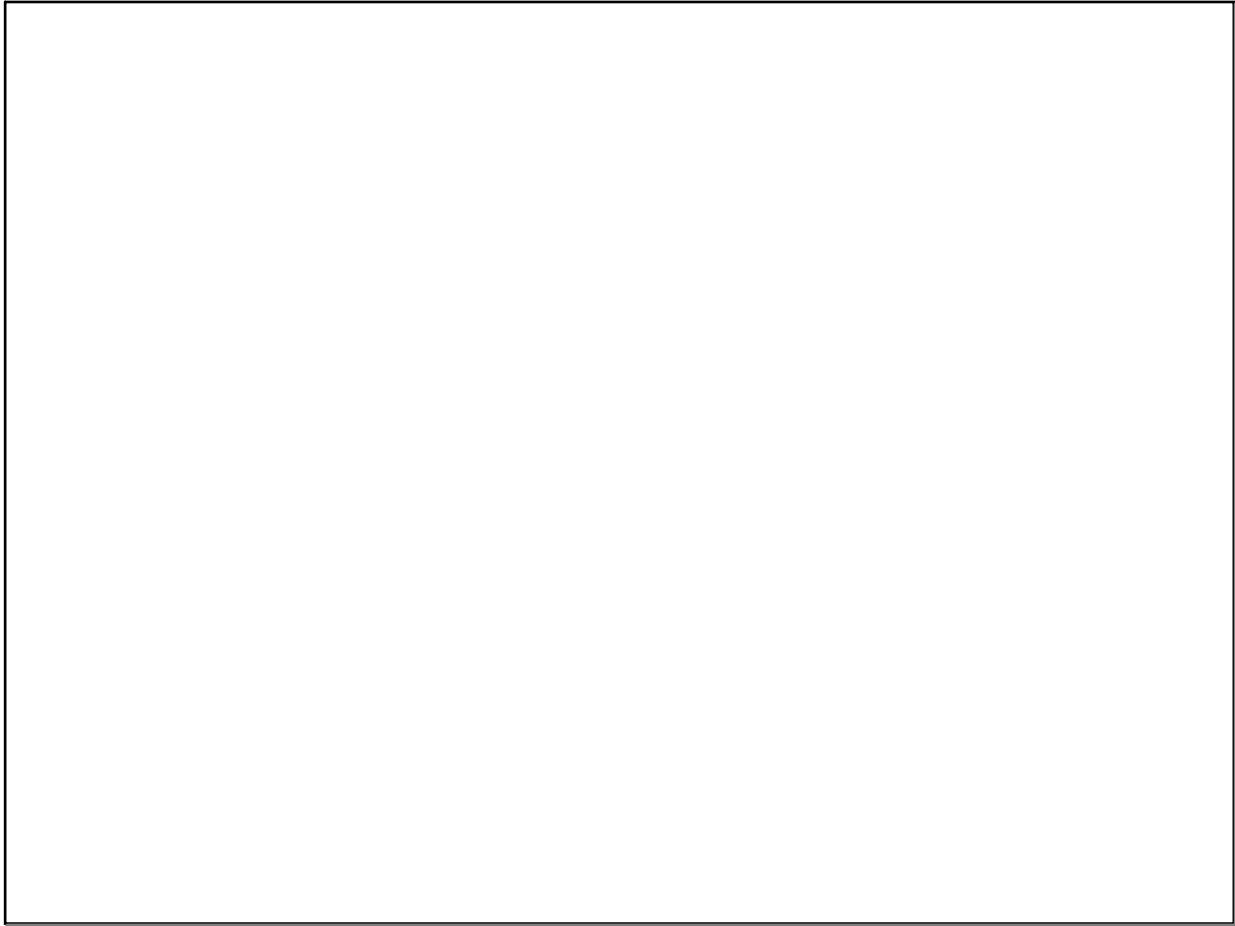
Look at #74 on page 542

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Homework 7-1: Wkst 7A



Jan 2-3:40 PM



Jan 22-7:13 AM